# EASTER: Learning to Split Transformers at the Edge Robustly

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Abstract-Prevalent large transformer models present signif-2 icant computational challenges for resource-constrained devices 3 at the Edge. While distributing the workload of deep learning 4 models across multiple edge devices has been extensively studied, 5 these works typically overlook the impact of failures of edge 6 devices. Unpredictable failures, due to, e.g., connectivity issues or 7 discharged batteries, can compromise the reliability of inference 8 serving at the Edge. In this article, we introduce a novel 9 methodology, called EASTER, designed to learn robust distri-10 bution strategies for transformer models against device failures 11 that consider the tradeoff between robustness (i.e., maintaining 12 model functionality against failures) and resource utilization 13 (considering memory usage and computations). We evaluate 14 EASTER with three representative transformers-ViT, GPT-2, 15 and Vicuna-under device failures. Our results demonstrate 16 EASTER's efficiency in memory usage, and possible end-to-end 17 latency improvement for inference across multiple edge devices 18 while preserving model accuracy as much as possible under 19 device failures.

<sup>20</sup> *Index Terms*—Deep learning (DL), design space exploration <sup>21</sup> (DSE), distributed inference, embedded system, robustness.

# I. INTRODUCTION

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S ARTIFICIAL intelligence (AI) continues to evolve rapidly, transformer models are increasingly prevalent in various applications [1]. Advanced pretrained models, such as BERT and GPT-4 [2], have spurred a range of novel tools, rincluding Copilot and ChatGPT. Typically, these models are executed on high-performance clusters with hundreds of GPUs, available as cloud services. However, the rise of Internet of Things (IoT) devices has driven a demand for deploying transformer-based tools at the Edge. Deploying these tools on edge or IoT devices offers significant advantages in terms of efficiency, security, and privacy. For example, a network of IoT devices in smart healthcare systems [3] within a hospital or a home setting, such as wearable health monitors, bedside

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monitors, and portable diagnostic devices, are equipped with 36 sensors to collect vital signs and patient data in real time. 37 By deploying deep neural networks, like transformer models, 38 directly onto these devices, the system can locally analyze 39 data, make immediate health assessments, or predict medical 40 events without the need to send or store sensitive patient 41 data in centralized cloud servers, thus enhancing user privacy 42 and data security. This also allows for faster, potentially life-43 saving decisions by reducing the latency associated with data 44 being sent to the cloud and the cloud processing of the data. 45 However, deploying transformer-based tools at the Edge presents 46 a significant challenge for edge or IoT devices due to the intensive 47 computational and memory requirements of transformer models. 48 For instance, the Vicuna-13B chatbot [4] requires 26 GB of 49 memory for the model parameters and substantial computational 50 resources for inference. 51

While constructing lightweight transformer models from 52 larger counterparts using methods like model compression [5] 53 or neural architecture search [6] is one approach, it often leads 54 to a reduced performance/accuracy score and resource-intensive 55 retraining of the newly derived models. In response, research 56 has focused on fully distributing transformer inference across 57 multiple edge devices without resorting to model compression 58 or cloud servers. Methods like model partitioning [7] and data 59 partitioning [8] have been explored to bridge the gap between 60 limited edge device resources and the demands of large trans-61 former models. Furthermore, by distributing the computational 62 workload of a transformer across multiple edge devices, the 63 system can operate more energy-efficiently, making it both cost-64 effective and sustainable for long-term deployment. However, 65 these methods generally assume continuous availability of all 66 participating devices, which is often unrealistic due to potential 67 device unavailability or failures. 68

Addressing this issue, our study emphasizes the need for 69 robust partitioning methods for distributed transformer infer-70 ence. Distributed inference across multiple devices offers a 71 promising solution for handling large transformer models (e.g., 72 Llama [9]) that exceed the memory capacities of individual 73 devices, such as IoT devices, smart surveillance cameras, 74 user laptops, etc. Existing frameworks, like Alpa [10] and 75 DeepSpeed [11], effectively support distributed large language 76 model (LLM) training, but do not address at all robust 77 distributed inference on edge devices and do not cater for 78 resource heterogeneity in edge systems or IoT settings. 79

Therefore, this article introduces a novel methodology, <sup>80</sup> called *EASTER*, designed to learn robust distribution strategies for transformers that ensure functional inference and <sup>82</sup>

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83 maintain close-to-original results under potential device fail-<sup>84</sup> ures. Learning such optimal strategies to distribute millions 85 of neurons is challenging because a vast and complex design 86 space needs to be explored. Typical transformer-based models 87 consist of several stacked encoder and decoder blocks. The 88 embedding dimension within each block, which represents 89 the size of vectors used to encode images, words, or tokens, <sup>90</sup> usually exceeds 100. For example, if the embedded dimension of an encoder block is 768 [12], and we consider each 92 dimension-related connection as a neuron, then the encoder 93 block has 768 neurons. If we want to distribute these 768 94 neurons over four devices evenly, the exact number of possible <sup>95</sup> distributions is  $\binom{768}{192} \times \binom{576}{192} \times \binom{384}{192}$ . The vast number of <sup>96</sup> potential possibilities to distribute just one encoder block 97 across multiple devices is almost unimaginable, let alone 98 when considering the distribution of multiple blocks in large <sup>99</sup> transformer models. There is a critical need to explore this 100 extensive design space efficiently to identify a neuron distri-<sup>101</sup> bution strategy that maintains performance against potential 102 device failures to ensure the robustness and reliability of the 103 distributed system.

For different distribution strategies (design points) of trans-104 105 formers in the vast space, our algorithm is designed to 106 efficiently and quickly explore and identify optimal design 107 points, enabling robust and memory-efficient splitting of 108 transformer models across multiple devices. We first narrow 109 down the design space by considering the neuron impor-110 tance in the transformer layers, as this assessment allows us 111 to group neurons within each layer, significantly reducing <sup>112</sup> their distribution complexity. Further, we achieve this by 113 adaptively and recursively splitting the design space into 114 several subspaces and learning the expected rewards associated 115 with different subspaces. To this end, we have developed a <sup>116</sup> variant of the upper confidence bounds applied to trees (UCT) <sup>117</sup> algorithm [13], aiming to enhance splitting and prioritizing 118 subspaces with the highest potential for robustness. By nav-<sup>119</sup> igating and sampling both the most and potential promising 120 subspaces rather than the entire vast space, our approach enhances search efficiency, while balancing exploration and 121 122 exploitation to avoid the pitfalls of local optima. The final 123 Pareto points/solutions offer an optimal blend of robustness 124 against device failures and operational efficiency regarding 125 computation and memory.

We also automate the process of dividing transformer 126 127 models for distributed computing by converting them into unified neural network intermediate representation (IR). 128 a 129 This step is followed by automated code generation and the 130 subsequent deployment of the models across multiple edge <sup>131</sup> devices. Our experimental results demonstrate that the system 132 configurations identified as Pareto-optimal points through the 133 aforementioned design space exploration (DSE) method not 134 only maintain system robustness but also achieve a notable 135 reduction in memory usage. Furthermore, these configura-136 tions reduce the end-to-end inference latency for very large 137 transformer models, demonstrating the effectiveness of our 138 approach in optimizing both the performance and efficiency 139 of distributed deep learning (DL) systems.

140 Our main novel contributions are summarized as141 follows.

- A novel UCT-based DSE algorithm is proposed that 142 efficiently narrows down the vast design space, facil- 143 itating the discovery of effective model partitioning 144 strategies for robust transformer distribution that balance 145 performance and resource usage. 146
- By empirical validation, we demonstrate the efficacy <sup>147</sup> of our *EASTER* methodology using typical transformers <sup>148</sup> like ViT-16 [12], GPT2-Large [14], and Vicuna-7B [4], <sup>149</sup> showcasing resilient model performance in image and <sup>150</sup> common reasoning tasks. <sup>151</sup>
- We provide the first implementation of an end-to-end 152 tool for splitting transformer models and also validate 153 the advantages of distributed inference in terms of 154 end-to-end inference latency and memory utilization 155 compared to single-device inference. 156

# II. RELATED WORK

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The proliferation of transformer models in various applications has necessitated their adaptation beyond the confines of powerful cloud computing resources, directing significant research interest toward edge deployments. This section reviews pertinent literature across three main themes relevant to our work on *EASTER*: 1) adaptation of large transformer models for resource-constrained edge devices; 2) resilience against device failures; and 3) efficiency in DSE. 165

# A. Adaptation of Transformer Models for Edge Constraints 166

The push toward deploying AI capabilities at the 167 edge, driven by privacy concerns, latency reduction, and 168 energy efficiency, has seen approaches like model compres- 169 sion [15], [16], [17] and neural architecture search [18], [19], 170 [20], [21] gain prominence. Such approaches can compress 171 original transformer models to smaller models for resource- 172 constrained devices. However, they typically require iterative 173 retraining and may result in accuracy loss. Another approach is 174 to deploy the original models onto distributed edge computing 175 platforms, such as health care systems [22], smart home 176 systems [23], etc., in order to leverage all available resources 177 collaboratively. Traditional layer and data partitioning methods 178 like [7] and [24] are applied to fully distribute the workload 179 of a large convolution neural network or a transformer- 180 based model among multiple edge devices, thereby reducing 181 the required computation resources of edge devices [25]. It 182 involves breaking down a model's computational graph into 183 smaller, manageable parts that can be processed in parallel 184 across multiple devices. This is particularly challenging in 185 edge computing due to the heterogeneous nature of devices 186 and their limited computational capabilities. Model parallelism 187 techniques like AlpaServe [10] developed for homogeneous 188 data center clusters are targets for multibatch inference which 189 would perform poorly for single batches in heterogeneous 190 edge environments. PipeEdge [24] partitions a neural network 191 model into multiple pipeline stages and applies a dynamic pro- 192 gramming (DP) algorithm to determine the optimal partition 193 scheduling strategy for heterogeneous computation and com- 194 munication. However, all of the aforementioned approaches 195 and methods assume that the involved edge computing devices 196 and communication links between them are always available 197

<sup>198</sup> and work properly. In contrast, our partitioning approach <sup>199</sup> not only aims at maintaining computational efficiency but <sup>200</sup> also considers the resilience of the system against possible <sup>201</sup> temporary or permanent failures of devices, an aspect often <sup>202</sup> overlooked in conventional partitioning strategies.

# 203 B. Resilience Against Edge Failures

Resilience against device failures at the Edge concerns the 204 205 property of a model being resilient in terms of inference accuracy to the failure of physical computing devices due 206 power outages, unstable interdevice connections, other 207 to hardware/software failures, etc. In distributed inference set-208 209 tings, the missing neurons mapped on those failed devices 210 may result in a significant accuracy drop of CNN or trans-211 former models [Fig. 1(b)]. Existing approaches and methods mitigate this risk introduce various strategies. The code 212 to 213 distributed computing (CDC) method proposed in [26] exemplifies an early attempt to enhance the resilience by utilizing 214 <sup>215</sup> an additional device to backup the computations of distributed 216 devices. This method effectively mitigates the impact of single 217 device failures but does not scale well to scenarios involving 218 multiple simultaneous device failures without introducing <sup>219</sup> excessive redundancy and associated computational overheads. 220 ElasticDL, introduced by Zhou et al. [27], represents a significant advancement by integrating fault tolerance and 221 elastic scheduling within a Kubernetes-native DL framework. 222 While ElasticDL enhances system resilience and adaptabil-223 224 ity, its practical deployment on edge devices is hampered 225 by Kubernetes' complexity and the limited computational 226 resources of edge environments.

In contrast to the aforementioned approaches, our method-227 228 ology EASTER introduces a comprehensive solution designed to enhance the resilience of transformer models in the face 229 of the unpredictable and dynamic nature of edge computing 230 environments. Unlike previous methods that often rely on 231 232 additional hardware resources, complex orchestration, or prior knowledge of potential failure types, EASTER employs a novel 233 partitioning strategy that inherently accommodates multiple 234 235 device failures without necessitating extra devices or computational redundancy. Our approach leverages advanced machine 236 learning techniques to adaptively distribute model computa-237 tions across edge devices, optimizing for both resilience and 238 <sup>239</sup> resource efficiency. By intelligently partitioning the model in 240 a manner that anticipates and mitigates the impact of device 241 failures, EASTER ensures robust inference accuracy under wide range of failure conditions without the limitations 242 a 243 imposed by specific assumptions or the need for supplemen-244 tary computational overhead.

# 245 C. Efficiency in Design Space Exploration

In the context of DSE, the original UCT algorithm [13], known for its efficacy in balancing the exploration– kexploitation tradeoff in single-objective optimization problems, is ingeniously adapted to the multiobjective optimization landscape in our work. This adaptation involves selecting promising parts of the search space by not see only leveraging the UCT's inherent strengths but also enhancing it with traditional machine learning techniques



Fig. 1. Comparative analysis of layer partitioning and its impact on memory reduction and for accuracy. (a) Layer partitioning method [7] with failures. (b) Top-1 accuracy versus memory reduction ratio.

for more efficient splitting and exploration of the design <sup>254</sup> space. Such an integration significantly augments the UCT <sup>255</sup> framework, enabling it to navigate complex, multidimensional <sup>256</sup> optimization problems with greater precision and efficiency. <sup>257</sup>

Existing DSE methods, such as the multiobjective 258 tree-structured Parzen estimator (MOTPE) [28] and the non- 259 dominated sorting genetic algorithm II (NSGA-II) [29], are 260 well known for their efficiency in multiobjective optimization. 261 MOTPE is renowned for its sample efficiency and capability 262 to handle high-dimensional spaces through its Bayesian 263 optimization framework, which is particularly beneficial in 264 scenarios with limited evaluation budgets. NSGA-II, on the other 265 hand, excels in finding a diverse set of solutions across the Pareto 266 front through its evolutionary algorithm, effectively managing 267 the tradeoffs between conflicting objectives. However, existing 268 methods fall short in adapting to our specific scenario, which 269 requires robust splitting of the transformer model block by block 270 while simultaneously optimizing memory usage and inference 271 latency. These methods lack customization for navigating the 272 vast design space of our scenario. 273

To address this gap, we enhance the UCT algorithm with <sup>274</sup> machine learning techniques to combine the UCT's dynamic <sup>275</sup> exploration–exploitation mechanism with the predictive and <sup>276</sup> generalization capabilities of machine learning. This not only <sup>277</sup> provides an efficient method to identify and explore promising <sup>278</sup> spaces but also enhances the algorithm's ability to adaptively <sup>279</sup> refine its search strategy based on learned insights. Our enhanced <sup>280</sup> UCT approach, when compared to methods like MOTPE and <sup>281</sup> NSGA-II, offers a complementary strategy ideally suited for <sup>282</sup> the search space is crucial. This tailored approach significantly <sup>284</sup> boosts our search efficiency and the quality of outcomes, making <sup>285</sup> it a particularly effective solution for our specific robustness <sup>286</sup> needs for splitting transformer models. <sup>287</sup>

## III. ROBUST MODEL SPLITTING

In this section, we provide an example to illustrate why 289 splitting a transformer model robustly is needed and why 290 DSE matters in this context. Moreover, we describe how 291 transformers can be splitted in a robust fashion. 292

# A. Motivational Example

The process of splitting a transformer model for distributed <sup>294</sup> inference across edge devices is crucial for running large mod- <sup>295</sup> els in environments with limited resources. Although some <sup>296</sup>

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<sup>297</sup> frameworks like PipeEdge [24] could distribute transformer 298 models across multiple IoT devices with orchestration, the 299 crux of the problem lies in the robustness of the pipeline 300 paradigm they utilize: a single failure within the pipeline can compromise the entire computation process. Thus, our discus-301 302 sion focuses on an alternative paradigm, namely, partitioning the layers themselves within a DL model across multiple 303 devices [7]. A transformer model, composed of N encoder 304 305 or decoder blocks, is designed for various tasks, such as 306 classification or text generation. As illustrated in Fig. 1(a), by <sup>307</sup> dividing blocks in the transformer model into two parts evenly, 308 specifically on a block-by-block basis, we can distribute its workload across two devices. Each device then processes its 309 310 allocated half blocks, necessitating periodic synchronization of 311 their intermediate results to maintain consistency throughout 312 the computation process. However, such a distribution strategy 313 still introduces a vulnerability: should one of the two devices 314 fail, it results in the loss of half the blocks' processing <sup>315</sup> capability, thereby significantly impacting the model's overall 316 performance and reliability. This scenario underlines the need 317 for a robust distribution strategy that can minimize the risk and impact of device failures. 318

Taking the ViT-16 transformer model [12] as an example, it 319 320 contains 12 encoder blocks stacked one by one. The significant 321 impact of a device failure on the model performance is <sup>322</sup> highlighted in Fig. 1(b). When splitting and distributing the 323 model's blocks across two devices, a device failure leads a substantial drop in Top-1 accuracy, as critical block to 324 325 information is lost. This scenario is graphically represented with Top-1 accuracy (red line) and memory reduction ratio 326 (blue line) against the number of distributed blocks (x-axis), 327 328 demonstrating that as more blocks are distributed instead of 329 fully replicated, the memory efficiency on the operational 330 device improves, but at the cost of reduced accuracy due to 331 the potential loss of computational resources during a device <sup>332</sup> failure. For instance, when distributing all 12 encoder blocks 333 of the ViT model across two devices, should one device fail 334 due to a power outage or disconnection, half of the weights 335 and intermediate results would be lost. In such a scenario, the 336 top-1 accuracy could drop to 20.95%, significantly impairing 337 the model performance of distributed inference.

This tradeoff between memory reduction and model accu-339 racy underlines the challenge: finding a method to split 340 encoder/decoder blocks that maximizes model accuracy reten-341 tion while achieving optimal memory efficiency. The goal 342 is to develop a strategy that ensures even if one or more 343 devices fail, the distributed model can maintain as much 344 of its original performance as possible. As mentioned in 345 Section I, given the vast design space for distributing neurons 346 in each encoder/decoder block, it is crucial to employ DSE 347 to identify the most efficient distribution pattern, aiming to 348 minimize accuracy loss while maximizing resource utilization 349 for optimal model deployment in distributed environments.

## 350 B. Robust Model Splitting

In the context of a transformer model containing N encoder <sup>352</sup> or decoder blocks, we introduce an innovative uneven splitting <sup>353</sup> method, called *Partial Split*, for distributing these blocks



Fig. 2. Partial split. (a) Even split. (b) Partial split.

across multiple devices with robustness in mind. This method <sup>354</sup> particularly aims at enhancing the model's resilience to device <sup>355</sup> failures while reducing the memory usage on each device. <sup>356</sup>

As illustrated in Fig. 2(a) for example, evenly distributing a <sup>357</sup> transformer block among four edge devices poses a significant <sup>358</sup> risk, namely, the model functionality is severely compromised, <sup>359</sup> for example, when three out of these four devices fail or lose <sup>360</sup> connection, as only a minimal fraction of attention connections <sup>361</sup> remains operational for inference. To address this vulnerability, <sup>362</sup> our method diverges from this conventional even splitting <sup>363</sup> approach. <sup>364</sup>

Instead, our method illustrated in Fig. 2(b) employs a strategic 365 replication of a certain fraction r of critical connections (the 366 yellow box) across multiple devices, based on their weight 367 importance. The remaining, less critical connections (the large 368 green box), constituting a (1 - r) fraction, are then evenly 369 distributed. This selective replication ensures that even in the 370 event of multiple device failures, the most vital connections 371 within each transformer block are retained, thereby preserving 372 the model functionality and inference capabilities to a large 373 extent. During runtime, the device initiating an inference request 374 for image classification or text generation tasks loads both the 375 replicated part (the yellow box) and its split part (the small 376 green box) of the model. The other devices in the network load 377 only their respective split parts. Notably, the replicated part 378 remains unloaded on these devices (the dotted yellow boxes). 379 This runtime loading strategy ensures that extra replicas are 380 not redundantly loaded on other devices, thereby optimizing 381 resource utilization and enhancing overall system efficiency. 382

# IV. PROBLEM FORMULATION

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The aforementioned uneven splitting method facilitates <sup>384</sup> robust distribution of the computational workload of a transformer model across edge devices. However, the limited <sup>386</sup> memory capacities of edge devices introduce challenges in <sup>387</sup> determining the optimal fraction *r* for each transformer block <sup>388</sup> that could preserve the model functionality and inference capabilities to a large extent. A large fraction *r* would require high <sup>390</sup> memory usage per device, potentially exceeding the memory <sup>391</sup> capacity of resource-limited edge devices. Conversely, a very <sup>392</sup> small fraction *r* might compromise the proper model functionality in case multiple devices fail. Thus, an important tradeoff <sup>394</sup> emerges between the memory usage per device and the model <sup>395</sup> functionality that is dependent on the fraction *r* of critical <sup>396</sup> connections that are replicated for each block. <sup>397</sup>

For a transformer model with *N* blocks, we define a <sup>398</sup> parameter set  $R = \{r_1, r_2, ..., r_N\}$ , where  $r_i \in [0..1]$  represents <sup>399</sup> the fraction of replicated connections for block *i*. Each set <sup>400</sup> of parameter values *R* corresponds to different memory usage <sup>401</sup>  $m_i$  per device  $D_i \in D$  and different model functionality in <sup>402</sup>



Fig. 3. Transformer partitioning.

<sup>403</sup> case some devices fail at runtime when a transformer model <sup>404</sup> is distributed over a set of edge devices *D*. Therefore, our <sup>405</sup> objective is to find an optimal set of parameter values  $R_{opt}$ <sup>406</sup> which maximizes the model accuracy or performance score in <sup>407</sup> case of failing devices with possible minimum memory usage <sup>408</sup> ( $m_1, m_2, \ldots, m_{|D|}$ ). Given the typically large value of *N* for <sup>409</sup> prevalent transformer models and the continuous range of  $r \in$ <sup>410</sup> [0..1], a vast and complex design space needs to be explored <sup>411</sup> in order to find an optimal solution.

# 412 V. EASTER METHODOLOGY

In this section, we present our novel methodology designed to learn robust distribution strategies for transformer models against device failures that consider the tradeoff between to robustness (i.e., maintaining model functionality against failures) and resource utilization (including memory usage and the computations). First, we provide more details about our robust partial split method introduced in Section III. Next, we present our DSE approach to solve the optimization problem, formutal tated in Section IV, that is required to achieve an efficient and robust partial split and distribution of transformer models on multiple edge devices. Finally, we introduce the end-to-end to we have developed to automate our robust partial split method and distributed deployment of transformer models.

#### 426 A. Partial Split Method for Transformers

In this section, we explain how the transformer model is split according to a parameter set *R*. Consider the example shown in Fig. 3 where *Block N* in a transformer model is distributed across two devices and the obtained fraction  $r_N \in R$ states for this example is 0.25.

The vital part of connections in the attention and feedforward blocks is represented by the two yellow boxes that are both replicated across the two devices. The remaining, lessvital part of connections for each block is split in two (the green boxes) and distributed evenly across the two devices.

To determine the vital part of connections, we calculate and use an importance score for each connection. For example, takuse an importance score for each connection. For example, takuse an importance score for each connections corresponding to this linear transformation using the Taylor score [30] as tag follows:

$$I_{W^k} = |\Delta \mathcal{L}| = \left| \mathcal{L}_{W^k} - \mathcal{L}_{W^k=0} \right| \approx \left| \frac{\partial \mathcal{L}}{\partial W^k} W^k \right|$$
(1)

<sup>444</sup> where  $I_{W^k}$  represents the importance score of the *k*th <sup>445</sup> connection/weights associated with the linear transformation, and  $|\Delta \mathcal{L}|$  represents the loss changes when we remove this 446 connection from the laver. After we calculate the importance 447 score of every connection in a layer, we sort the connections 448 based on the importance score in descending order, thereby 449 creating a separate sorted list for every layer. If the target 450 fraction of replicated connections for a layer is r then we 451 start from the beginning of the sorted list and take the first 452 r% of the connections, thereby classifying them as vital. The 453 rest are classified as less vital. Furthermore, it is crucial to 454 understand that when we find that nearly all connections in 455 a layer have similarly high importance scores (i.e., nearly all 456 are vital), the DSE process (see Section V-B) is designed to 457 adjust the fraction value r of this layer close to 1.0, instead  $_{458}$ of maintaining the initial value. This adjustment is crucial 459 to preserve and replicate the layer as much as possible to 460 avoid significant performance degradation. During the (design- 461 time) DSE process, the sets of small r values for important 462 layers or blocks, leading to a considerable drop in model 463 performance, are automatically categorized into less promising 464 subspaces. This mechanism ensures that our DSE process 465 systematically avoids configurations that would negatively 466 impact the model's effectiveness significantly. This adaptive 467 approach ensures that our method retains crucial connectivity 468 to effectively retain model performance. Below, we provide 469 details on how our partial split method is further tailored for 470 the attention and feedforward blocks within the transformer 471 architecture to efficiently reduce computational workload and 472 memory usage when the transformer is distributed across 473 different edge devices. 474

1) Attention Block: As depicted in Fig. 3, the hidden states 475  $H_{i-1}$  coming from the previous transformer block are trans- 476 formed into queries (Q), keys (K), and values (V) using the  $_{477}$ weight matrices  $W_q$ ,  $W_k$ , and  $W_v$ . Our method splits these 478 matrices along their column dimensions (denoted by  $W_a^c$ ,  $W_k^c$ , 479 and  $W_{\nu}^{c}$ ) and distributes them across devices. Consequently, 480 each device generates the corresponding segments of Q, K, and 481 V (denoted by the yellow and green boxes), necessitating an  $_{482}$ all-gather communication operation to concatenate the corre- 483 sponding segments into complete Q, K, and V tensors. Taking 484 the linear transformation with  $W_q$  weights (Fig. 3) in the 485 attention block as an example, the query matrix Q is generated 486 by  $W_q$ . If the embedded dimension of the input tensor  $H_i$  is D, 487 we compute the D importance scores for query Q using (1). 488 Once the replication factor  $r_i$  is determined, we rank and 489 split the  $W_q$  weights along its column dimensions based on 490 the rank indices derived from the D scores. We choose to 491 replicate the top r% of weight  $W_q$  and allocate the remaining 492 (1 - r)% to multiple devices. For the small portion of  $W_{a}$  493 on each device, we replace the original matrix multiplication 494 (matmul) operation with a small matmul operation containing 495 its corresponding different part of weight  $W_q$ . To maintain 496 output accuracy, a communication operation for gathering the 497 partial Q output is added after the small matmul. After the 498 attention block multiplies the attention scores with values 499 (V), the linear transformation with weight matrix  $W_0$  maps 500 the multiplication result to match the dimension size of the 501 intermediate output. In our method, we also split  $W_o$  into 502 segments along the column dimension. Each segment of  $W_{0}^{c}$  503 produces a partial part of the intermediate output. Similarly, an 504

<sup>505</sup> extra all-gather communication operation is added to collect <sup>506</sup> the segments and ensure the correctness.

Apart from these layers, the embedding layer follows a similar strategy for its matmul operation. However, we abstain from applying our partial split method to layernorm layers due to their relatively minimal weight and computational demand. Importantly, the full replication of layernorm weights on each bit device is prioritized to ensure model stability, given their significant role [31].

2) Feedforward Block: This block within a transformer 514 515 block involves two linear transformations with weight matrices  $W_1$  and  $W_2$  to process the intermediate output and generate the 516 517 hidden states  $H_i$  going to the subsequent transformer block. 518 The first weight matrix is split along the column dimension 519 (denoted as  $W_1^c$  in Fig. 3). The second weight matrix is split along the row dimension (denoted as  $W_2^r$ ). The partial <sub>521</sub> output tensors (the yellow and green boxes) produced by  $W_1^c$ 522 can directly go through the nonlinear activation and serve 523 as the input for the second linear transformation which is s24 also split and denoted as  $W_2^r$ . This design eliminates the 525 need for an all-gather operation to concatenate the partial 526 outputs produced by the first linear transformation, thereby 527 reducing both the computational workload per device and the 528 interdevice communication overhead. Finally, a collective all-529 reduce operation is applied to sum the partial output from all 530 devices to form the correct hidden states output  $H_i$ .

#### 531 B. Design Space Exploration

To solve the optimization problem formulated in Section IV, 532 we have devised a DSE approach that effectively navigates in 533 <sup>534</sup> the vast and complex design space mentioned in Section IV. 535 Our DSE approach leverages supervised learning techniques 536 to progressively concentrate the search for an optimal solu-537 tion within increasingly smaller and more promising spaces, 538 thereby enhancing search efficiency. As depicted in Fig. 4, 539 the approach starts by randomly generating several design 540 points  $\mathbb{R} = \{R_1, R_2, \dots, R_p\}$  (yellow points), and evaluate the objectives  $\mathbb{F}(\mathbb{R})$  using the fitness function  $\mathbb{F}$  for each 541 542 design point  $R_i \in \mathbb{R}$  to form an initial learnable space =  $(\mathbb{R}, \mathbb{F}(\mathbb{R}))$ . Here,  $R_i = \{r_1^i, r_2^i, \dots, r_N^i\}$  is a set of 543 D 544 fractions corresponding to a specific partial split strategy for all N blocks in a transformer model. The fitness function 545 concerns the evaluation of various conflicting objectives, 546 F 547 such as memory usage, energy consumption, performance, 548 etc. It can be implemented using analytical models, real 549 measurements, etc. In this article, our fitness function is based 550 on real measurements to ensure an accurate and practical <sup>551</sup> evaluation of the objective values. Taking the ViT-16 model as 552 an example, we directly measure the peak memory usage on <sup>553</sup> real devices during run-time, and we take the Top-1 accuracy 554 of the ImageNet-1K validation dataset as the performance <sup>555</sup> metric. Then, our DSE approach recursively splits the design <sup>556</sup> space D and obtains a set of split boundaries. Subsequently, we <sup>557</sup> apply these learned boundaries to generate new design points <sup>558</sup> within specific promising design spaces to improve the search 559 efficiency. We apply the calculation equation in line 24 of 560 Algorithm 1 to identify which area within  $\mathbb{R}$  is most likely to <sup>561</sup> contain optimal design points and then concentrate our search



Fig. 4. Our DSE approach.

on this smaller, promising area, denoted as  $D_P^*$  and shown 562 in the middle of Fig. 4. However, an early decision about 563 the promising area might inadvertently overlook other areas 564 that could contain optimal points as well. To mitigate this, 565 while the majority of our design points are generated within 566 the currently perceived promising area  $D_P^*$ , we also allocate a 567 smaller portion of design points to generate from other spaces, 568 represented by  $D_S^*$ . This approach iteratively learns the entire 569 space  $\mathbb{R}$  and allows us to more accurately identify the most 570 promising regions for optimal points. 571

Algorithm 1 describes, in more detail, the aforementioned 572 DSE approach illustrated in Fig. 4. The algorithm consists of 573 two main steps and takes as an input the maximum search 574 trials T, the number of new random design points  $n_p$  for 575 updating the search space D, a lower bound (lb) to determine 576the maximum number of design points in an unsplittable area, 577 and the exploration factor  $\alpha$  which determines the degree of 578 exploration. A higher value for  $\alpha$  encourages more exploration 579 in the search space. The output of Algorithm 1 is space 580  $D_P = \{(R_1, F_{R_1}), \dots, (R_{|P|}, F_{R_{|P|}})\}$  of Pareto-optimal solutions 581 where every solution  $R_i = \{r_1^i, r_2^i, \dots, r_N^i\}$  is a set of fractions 582 corresponding to a Pareto-optimal partial split strategy for 583 all N blocks in a transformer model. In line 1, we first 584 randomly initialize a number of design points and evaluate 585 their objectives using the fitness function, yielding an initial 586 learnable search space D. 587

In step 1 (lines 3–8), the algorithm narrows down the space <sup>598</sup> via support vector machine (SVM) classifiers and generates <sup>599</sup> a series of SVM boundaries. In lines 3–6, we select the <sup>590</sup> nondominated points from *D* to create a new primary space <sup>591</sup> marked as  $D_P$ , and the rest of the points are put into a <sup>592</sup> new secondary space marked as  $D_S$ . In lines 7 and 8, the <sup>593</sup> *NarrowDown* function is applied to recursively split  $D_P$  and <sup>594</sup>  $D_S$  into smaller spaces  $D_P^*$  and  $D_S^*$ . Concurrently, all involved <sup>595</sup> splitting SVM boundaries are aggregated into the boundary <sup>596</sup> sets  $\mathbb{CL}_P$  and  $\mathbb{CL}_S$ .

In step 2 (lines 9–12), we generate new design points <sup>598</sup> and evaluate these new design points using the fitness <sup>599</sup> function FITNESS. To balance the exploration–exploitation <sup>600</sup> tradeoff, 80% of these new points ( $\mathbb{R}_P$ ) are derived from  $D_P^*$  <sup>601</sup> in line 9, while the remaining 20% (i.e., for  $\alpha = 0.2$ ) of the <sup>602</sup> new design points ( $\mathbb{R}_S$ ) are derived from  $D_S^*$  in line 10. This <sup>603</sup> ratio, while adjustable, typically requires experimental trials <sup>604</sup> for better search efficiency. Then, we apply the fitness function <sup>605</sup> to evaluate the objective values for these new points and add <sup>606</sup> them to the search space *D* in line 12. This iterative process is <sup>607</sup> repeated until the maximum number of trials *T* is reached (see <sup>608</sup> line 2). Ultimately, the Pareto-optimal points comprising space <sup>609</sup>  $D_P$  found by this DSE process represent the optimal solutions <sup>610</sup> that balance the memory usage and the model functionality. <sup>611</sup>

643

```
Algorithm 1: DSE
    Input : Maximum trials T; Population size n_p; lb,
                  exploration factor \alpha;
    Output: Space D_P with Pareto points;
 1 Initialize randomly D with points (R, F_R):
      D \leftarrow \{(R_1, \text{FITNESS}(R_1)), \cdots, (R_{n_p}, \text{FITNESS}(R_{n_p}))\}
2 while |D| \leq T do
          // Step 1: Narrow Down Search Space
          foreach (R_i, F_{R_i}) \in D do
3
               if F_{R_i} is nondominated then
4
                D_P \leftarrow D_P \cup (R_i, F_{R_i})
5
          D_S \leftarrow D \setminus D_P; \ \mathbb{CL}_P \leftarrow \emptyset; \ \mathbb{CL}_S \leftarrow \emptyset
6
          D_P^*, \mathbb{CL}_P = \text{NarrowDown}(D_P, \mathbb{CL}_P)
7
          D_{S}^{*}, \mathbb{CL}_{S} = \text{NarrowDown}(D_{S}, \mathbb{CL}_{S})
 8
          // Step 2: Add New Random Points,
                                Evaluate and Update D
          11
          \mathbb{R}_P = \text{NewPoints}((1 - \alpha) * n_p, \mathbb{CL}_P)
9
          \mathbb{R}_S = \text{NewPoints}(\alpha * n_p, \mathbb{CL}_S)
10
          foreach R_i \in (\mathbb{R}_P \cup \mathbb{R}_S) do
11
                 D \leftarrow D \cup (R_i, \text{FITNESS}(R_i))
12
13 return D_P
14
   Function NarrowDown (D, \mathbb{CL}):
15
          foreach (R_i, F_{R_i}) \in D do
16
             \mathbb{R}_D \leftarrow \mathbb{R}_D \cup R_i
17
          (\mathbb{R}_{D_1}, \mathbb{R}_{D_2}) = KMeansTwoClustersOn(\mathbb{R}_D)
18
          D_L = (\mathbb{R}_{D_1}, 1) \cup (\mathbb{R}_{D_2}, -1)
19
          CL, D_1, D_2 = SVMTrainedOn(D_L)
20
          if (|D| < lb) \lor (CL(D_1) = CL(D_2) then
21
               return D, \mathbb{CL}
22
          else
23
               UCB(\mathbb{R}_{D_i}) = \overline{\mathbb{F}(\mathbb{R}_{D_i})} + \alpha \sqrt{\frac{\log |\mathbb{R}_{D_i}|}{|\mathbb{R}_{D_i}|}}: i = 1, 2
24
               \mathbb{R}_{D^*} = \operatorname{argmax} \operatorname{UCB}(\mathbb{R}_{D_i}); \ D^* = (\mathbb{R}_{D^*}, \mathbb{F}(\mathbb{R}_{D^*}))
25
                              \mathbb{R}_{D_i}
               \mathbb{CL} \leftarrow \mathbb{CL} \cup \mathrm{CL}
26
               return NarrowDown (D^*, \mathbb{CL})
27
28 Function NewPoints (N, \mathbb{CL}):
29
          \mathbb{R} \leftarrow \emptyset
          while |\mathbb{R}| < N do
30
               R = RandomPoint;
31
               \mathbb{R} \leftarrow \mathbb{R} \cup R
32
               foreach CL_i \in \mathbb{CL} do
33
                     if CL_i(R) = -1 then
34
                           \mathbb{R} \leftarrow \mathbb{R} \setminus R
35
                           break
36
          return \mathbb{R}
37
```

In lines 15–27, the *NarrowDown* function recursively splits the search space D and obtains a series of learned split boundaries  $\mathbb{CL}$ . In line 18, we initially employ the *K*-means clustering method to categorize/divide the design points within  $\mathbb{R}_D$  into two distinct clusters  $\mathbb{R}_{D_1}$ ,  $\mathbb{R}_{D_2}$ . Following



Fig. 5. Multinode IR conversion tool.

this clustering, we calculate the average objective values for 617 each cluster. The cluster with the higher average objective 618 values is considered to be situated in a more favorable space. 619 Consequently, in line 19, we assign a label of 1 to the design 620 points in this more promising cluster, while design points in 621 the less favorable cluster are labeled as -1, and we put all 622 labeled points in a new set  $D_L$ . In line 20, we train the SVM 623 classifier CL with the new set of labeled points  $D_L$  and split 624  $D_L$  into two spaces  $D_1$  and  $D_2$ . In lines 21 and 22, if the 625 number of design points in D is below the lower bound lb or 626 if the SVM classifier CL predicts only a single category, both 627 indicating that space D is nondivisible, the recursive function 628 NarrowDown terminates and returns the set of classifiers  $\mathbb{CL}$ . 629 Otherwise, in lines 24–26, we mark the space with the larger 630 UCB value [13], calculated in line 24, as the more promising 631 design space  $D^*$ , and add the SVM classifier CL into the 632 recursive splitting set  $\mathbb{CL}$ . 633

In lines 28–37, the *NewPoints* function randomly generates <sup>634</sup> *N* new design points using the input set of SVM classifiers  $\mathbb{CL}$ . <sup>635</sup> In lines 31 and 32, a random design point *R* is generated and <sup>636</sup> added to the set of new points  $\mathbb{R}$ . Then, point *R* is classified <sup>637</sup> using the set of trained SVM classifiers  $\mathbb{CL}$  in lines 33–36. <sup>638</sup> That is, if all SVMs in  $\mathbb{CL}$  classify point *R* to belong to the <sup>639</sup> class with label 1 then point *R* remains in the set; otherwise, it <sup>640</sup> is removed (line 35). Finally, in line 37, the new set of random <sup>641</sup> points  $\mathbb{R}$  is returned. <sup>642</sup>

# C. Multinode Intermediate Representation

We have developed an end-to-end tool that facilitates automated model partitioning and its distributed deployment, in line with one of the Pareto-optimal partial split strategies  $R_i \in 646$  $D_P$  found by our DSE Algorithm 1 presented in Section V-B. 647 In general, traditional frameworks for DL model deployment 648 on edge devices, such as TVM [32], IREE [33], and others, 649 do not sufficiently support distributed inference. Therefore, 650 our end-to-end tool is implemented to transform CNNs or 651 transformer models from Huggingface [34] into optimized 652 multinode computation graphs, thereby making them suitable 653 for efficient deployment across multiple devices. Our tool 654 is versatile enough to support both CNNs and transformer 655 models but in this article we focus on its application to 656 transformer models. 657

As illustrated in Fig. 5, our tool begins by utilizing the 658 existing "torch.compile" [35] method to convert an initial 659 PyTorch transformer model into the low-level ATen IR for a 660 single node. Subsequently, an automated conversion process 661 is employed to replace the single-node ATen IR into a multin-662 ode variant. For instance, in handling linear transformations, 663 the tool splits the associated coefficients and redefines new 664 665 Linear transformations that are adapted to the altered shapes 666 of coefficients or inputs as illustrated by the red boxes 667 in Fig. 5. Modifications to these operations are facilitated 668 using "torch.fx" [36], accommodating the new coefficient 669 dimensions. Our own customized multinode communica-670 tion operations, such as GatherByIndex, AllReduceByIndex, AllConcatByIndex, etc., are integrated after the modified 671 672 operation (see red box "Linear" in Fig. 5) to ensure the 673 calculation correctness. To enhance the tool's versatility, we 674 implement these communication operations in C++ such 675 that they can be integrated into other inference engines. We 676 have also developed a compatible interface that enables the 677 conversion of this multinode IR into formats supported by 678 various other inference engines (e.g., NCNN [37], IREE, 679 etc.). Its compatibility and ease of integration with these 680 existing edge frameworks enhances both usability and scalability. Additionally, a robust fault handler is incorporated 681 682 to ensure reliable execution during distributed inference, pro-<sup>683</sup> viding resilience against potential device failures or network disruptions. An inner timeout mechanism governed by peri-684 685 odic heartbeats [38] can prevent the distributed system from 686 deadlocks that might arise due to device failures or other 687 operational anomalies.

# 688 VI. EVALUATION OF OUR EASTER METHODOLOGY

In this section, we evaluate our *EASTER* methodology to demonstrate its efficacy on typical transformer models and showcase resilient models' performance. We describe our experimental setup followed by presenting and discussing some experimental results obtained during automated DSE evaluation experiments, we have performed using Algorithm 1 and the end-to-end tool introduced in Section V-C.

# 696 A. Experimental Setup

To evaluate EASTER, we perform experiments with three typ-697 698 ical transformer models, namely, ViT-16 [12], GPT2-Large [14], 699 and Vicuna-7B [4] representing three different kinds of 700 transformer architectures, taken from the Huggingface open-<sup>701</sup> source community [34]. Given their widespread use in image 702 and text tasks, and their diversity in transformer blocks, 703 operation counts, and memory requirements, we consider these 704 transformers to be representative targets to demonstrate the <sup>705</sup> merits of our methodology. We compare the searching efficiency 706 of our Algorithm 1 on these models with two state-of-the-art 707 multiobjective optimization algorithms, namely, the NSGA-II <sup>708</sup> Genetic Algorithm [29] and MOTPE [28]. The task of our 709 DSE experiments is to simultaneously minimize the maximum 710 memory usage per device and the model performance score 711 (loss) under severe device failures. To ensure a fair comparison with NSGA-II and MOTPE, we set the maximum number 712 713 of search iterations to 2500 for each DSE experiment. The 714 searching time for the three methods are quite similar, with the 715 majority of time being consumed by the objective evaluations. <sup>716</sup> For the first objective (maximum memory usage per device), we normalize its value range to [0, 1] by dividing the memory usage <sup>718</sup>  $m_i(R_i)$  by the total memory usage on a single device  $D_i$ . Lower 719 values indicate reduced replication and more balanced model 720 distribution. To evaluate the second objective (performance score *S*) of the models, we employ distinct techniques tailored 721 to each model's specific domain. For the ViT-16 model, we 722 measure the Top-1 error score on the ImageNet-1k dataset for 723 image tasks. A lower error represents higher image classification 724 capabilities, and the lower the error the better. For the two LLMs 725 (GPT2-Large and Vicuna-7B), we utilize zero-shot perplexity 726 (PPL) analysis on the WikiText2 and PTB datasets to assess the 727 models' language understanding and generalization capabilities. 728 A lower PPL score, especially in a zero-shot context, means a 729 better ability to handle unseen data. 730

To validate the performance of Pareto-optimal points from 731 the DSE process using Algorithm 1, we apply the split 732 fractions  $R_i$ , found by the algorithm, to the two LLMs by 733 distributing each LLM across four devices, i.e., four GPU 734 units in our experiments. We disable three GPU units to 735 simulate severe device failure scenarios in order to assess the 736 models' robustness. We apply a separate and more diverse 737 collection of reasoning and generative datasets [39] to test the 738 models' performance (robustness) against severe failures in 739 practical reasoning tasks, namely, ARC-easy, ARC-challenge, 740 WinoGrande, HellaSwag, BoolQ, PIQA, and OpenbookQA. 741 These diverse datasets provide a comprehensive platform for 742 testing the models' reasoning and generative capabilities. 743

To evaluate the resilience of our methods under varying failure 744 conditions, we deployed three models across four edge devices 745 and examined model performance in scenarios where 1 (1D-746 Fail), 2 (2D-Fail), or 3 devices (3D-Fail) experience failures. We 747 take the state-of-art layer partitioning method (LP) [7] from the 748 domain of distributed CNN inference as inspiration to implement 749 a similar method for linear operations within encoder/decoder 750 blocks of transformer models. Subsequently, we benchmark 751 this LP-inspired partitioning method, which does not utilize 752 the notion of neuron importance, against our approach in terms 753 of robustness. For the three transformer models, we assess the 754 robustness of our method using different sets of R values for the 755 partial split strategy, allowing for a comprehensive comparison 756 of how well each method retains model performance against 757 device failures. 758

To actually test distributed inference for transformers across 759 multiple edge devices, our experimental edge test-bed consists 760 of eight NVIDIA Jetson Xavier NX devices connected over 761 a 1000-Mb/s network router. Each device has an embed-762 ded MPSoC featuring a 6-core Carmel ARMv8.2 CPU, an 763 NVIDIA Volta GPU with 384 CUDA cores, 48 Tensor cores, 764 and 8 GB of LPDDR4x memory. We demonstrate the func- 765 tionality of our multinode implementation, generated by our 766 end-to-end tool introduced in Section V-C, and the advantages 767 of distributing large transformer models over multiple edge 768 devices/boards by conducting a series of benchmarks on 769 the aforementioned edge test-bed using the three representa-770 tive transformer models ViT-16, GPT2-Large, and Vicuna-7B 771 under four different distributed system configurations: single 772 device, two devices, four devices, and eight devices. In all 773 experiments, transformer blocks were evenly distributed across 774 the devices. We mainly evaluate two metrics: 1) overall end-to-775 end inference latency and 2) memory reduction with different 776 distribution configurations. 777

The end-to-end latency (T) of a model is measured from the 778 time a user input is received until the time the complete output 779

 TABLE I

 Execution Time of Main Steps in EASTER

	Importance Calculation		Evaluation Time Per DSE Tria		
	CPU (s)	GPU (s)	CPU (s)	GPU (s)	
ViT-16	200.90	4.15	2480.30	156.73	
GPT2-Large	43.35	4.70	35.48	4.65	
Vicuna-7B	430.42	8.44	48.742	7.82	

780 is generated. For the ViT-16 model, user inputs are images with dimensions  $(3 \times 224 \times 224)$ , whereas for the two LLMs 782 (GPT2-Large and Vicuna-7B), user inputs are sequences of 783 128 tokens. The reported latency is computed by averaging The time T for 100 user inputs. To measure T and break it down to 785 computation time  $(T_{cal})$  and communication/synchronization 786 overhead  $(T_{\text{comm}})$  in our distributed inference execution, we employ a specific adjustment of the timeout parameter values 787 788 in our multinode communication operations introduced in Section V-C. More specifically, setting the timeout values 789 790 to zero permits each device to function independently, i.e., without interdevice data communication and synchroniza-791 792 tion delays, thereby enabling the measurement of the pure rg3 computation time  $T_{cal}$ . Altering the timeout values to one sec-794 ond activates interdevice communication and synchronization 795 actions besides the pure computations, thereby facilitating the 796 measurement of the total end-to-end inference latency T. We 797 then determine the communication/synchronizaton overhead <sup>798</sup>  $T_{\text{comm}}$  by calculating the difference  $T-T_{\text{cal}}$ , thereby effectively 799 quantifying the additional time needed for interdevice data 800 communication and synchronization.

To determine the aforementioned memory reduction, we continuously monitor the peak memory usage of each device in every distributed system every distributed system configuration.

# 805 B. Execution Time Evaluation of the EASTER Method

We evaluate the execution time of the main steps of our *EASTER* method on two different hardware platforms, namely, a platform based on an Intel Core i9-13900K CPU and a platform based on an NVIDIA H100 SXM5 GPU. For each transformer model, we measure the time required to calculate the importance still scores of connections within the model as well as the time to evaluate a single design point during the DSE process.

The importance score calculation is performed only once. 813 814 Illustrating this calculation for the ViT-16 model, we randomly 815 take 50 samples from the ImageNet-1K training dataset where 816 each sample is a batch of 128 random images. Using each <sup>817</sup> sample and the ViT-16 model, we apply (1) to calculate <sup>818</sup> an importance value for every connection within the model, 819 i.e., we calculate 50 values per connection in total. Then, we 820 compute the average of these 50 values for each connection 821 and use this average value as the importance score of the 822 connection in our DSE process. For the GPT2-Large and Vicuna-7B transformer models, the importance scores are 823 824 calculated similarly through 50 random samples from the 825 language datasets. The time required to execute the importance 826 score calculation for the three transformer models is shown 827 in Columns 2 and 3 of Table I. For example, on the GPU-828 based platform, the complete set of importance scores of all connections in the ViT-16 model is computed in just 4.15 s. <sup>829</sup> Computing the same set of scores on the CPU-based platform <sup>830</sup> takes 200.9 s. In Columns 4 and 5 of Table I, we provide the <sup>831</sup> evaluation time for a single design point in our DSE process. <sup>832</sup> For example, on the CPU-based platform, evaluating the Top-1 accuracy of the ViT-16 model takes approximately one hour <sup>834</sup> to complete. Conversely, the powerful GPU platform validates <sup>835</sup> the Top-1 accuracy for a specific design point in under 3 min. <sup>836</sup>

#### C. DSE Results and Comparison

We have performed three distinct DSE experiments for the ViT-16, GPT2-Large, and Vicuna-7B models by employing our *EASTER* methodology and Algorithm 1 along with the NSGA-II and MOTPE algorithms for comparison purposes. The Pareto-optimal points found by each of these three algorithms are separately plotted in Fig. 6. The yellow triangles represent the points found by MOTPE, the blue crosses represent NSGA-II points, and the red dots correspond to points found by our Algorithm 1 within *EASTER*. The *x*-axis in Fig. 6(a)–(c) represents the normalized maximum memory usage per device explained in Section VI-A. The *y*-axis represents the Top-1 error for ViT-16 and the PPL for GPT2-Large and Vicuna-7B. The rationale behind using the Top-1 error and PPL is explained in Section VI-A.

To quantitatively assess the effectiveness of *EASTER*, <sup>853</sup> NSGA-II, and MOTPE, as well as to compare them, we <sup>854</sup> calculate the well known and widely used hypervolume metric <sup>855</sup> (hv), based on the Pareto-optimal points plotted in Fig. 6, <sup>856</sup> that serves as an indicator of the search space coverage <sup>857</sup> in DSE. As shown in Fig. 6, our *EASTER* methodology <sup>858</sup> and algorithm demonstrate superior performance because of <sup>859</sup> the higher hypervolume value hv, indicating more effective <sup>860</sup> search space coverage of *EASTER* compared to NSGA-II <sup>861</sup> and MOTPE. For example, the Pareto-optimal points found <sup>862</sup> by *EASTER* for Vicuna-7B and shown in Fig. 6(c) dominate <sup>863</sup> those found by NSGA-II and MOTPE, resulting in higher <sup>864</sup> hypervolume value of 3.24 and highlighting the *EASTER* <sup>865</sup> effectiveness in identifying optimal solutions. <sup>866</sup>

As explained in Section VI-A, we apply the split fractions  ${}^{867}$  $R_i$ , found by Algorithm 1, to the models by distributing each  ${}^{868}$ model across four devices. Moreover, we disable *three of*  ${}^{869}$ *the four* devices in order to simulate severe device failure  ${}^{870}$ scenarios to assess the models' robustness. The results for the  ${}^{871}$ LLMs (GPT2-Large and Vicuna-7B) are shown in Table II.  ${}^{872}$ 

The first column specifies three different  $R_i$  settings for <sup>873</sup> each of the two LLMs together with the baseline setting, <sup>874</sup> named R = 1. The baseline setting R = 1 for each LLM <sup>875</sup> is the original model fully replicated over the four devices <sup>876</sup> with no loss of model weights/connections due to failures. <sup>877</sup> Note that the evaluation metrics associated with settings A– <sup>878</sup> C are also shown in Fig. 6(b) and (c)—see the red dots <sup>879</sup> marked with A–C. The second column in Table II shows <sup>880</sup> the maximum memory usage per device under the aforementioned settings. The remaining columns show the evaluation <sup>882</sup> i.e., the part still running on the nonfailing device, across <sup>884</sup> several zero-shot open-ended tasks on widely recognized <sup>885</sup>

838



Fig. 6. Comparison of DSE results delivered by EASTER, NSGA-II, and MOTPE for (a) ViT-16, (b) GPT2-Large, and (c) Vicuna-7B.

 TABLE II

 Zero-Shot Performance (Max. Per-Device Memory Usage and Accuracy-%) With Three Out of Four Edge Devices Failing

Models	Memory (reduction ratio)	ARC-c	ARC-e	WinoGrande	HellaSwag	OBQA	PIQA	BoolQ
Vicuna-7B (A) Vicuna-7B (B)	9.24 GB(-65.80%) 13.06 GB(-51.60%)	21.93	33.71 44 49	52.25 57.14	29.36 34 39	17.00 20.60	57.73 64 58	62.14 62.17
Vicuna-7B (C)	20.65 GB(-23.50%)	38.31	67.97	67.56	50.40	28.20	72.96	79.05
Vicuna-7B (R=1)	27.00 GB(baseline)	43.17	75.63	69.46	56.48	33.00	77.31	80.98
GPT2-Large (A)	1.08 GB/(-66.20%)	19.54	29.88	50.12	26.41	12.60	55.28	54.22
GPT2-Large (B)	1.72 GB/(-46.10%)	19.54	33.96	49.49	28.39	11.60	59.85	60.92
GPT2-Large (C)	2.42 GB/(-24.50%)	18.86	44.61	53.35	31.89	18.00	65.45	62.05
GPT2-Large (R=1)	3.20 GB/(baseline)	21.67	53.16	55.33	36.40	19.40	70.35	60.49

common sense reasoning datasets [39]: ARC-e(asy), ARCc(hallenge), WinoGrande, HellaSwag, BoolQ, PIQA, and
OpenBookQA.

Analyzing the results in the second column of Table II, we 889 <sup>890</sup> observe that the memory reduction for setting C with  $R \approx 0.75$ <sup>891</sup> compared to the baseline clearly shows that the accuracy loss <sup>892</sup> is relatively small. The memory reduction for settings A and B <sup>893</sup> in this worst-case scenario (3D-Fail) confirms the efficacy of our EASTER methodology. For example, the Vicuna-7B model 894 <sup>895</sup> experiences a significant memory reduction of up to 65.80% <sup>896</sup> (from 27.00 to 9.24 GB), but still retains competitive accuracy 897 compared to the original GPT2-Large model across several 898 evaluated tasks like WinoGrande and BoolQ. Although the 899 memory reduction comes with a certain accuracy tradeoff, 900 especially for tasks like ARC-c, ARC-e, etc., this remains within an acceptable range given the significant benefits 901 902 of reduced memory demands and improved computational efficiency across multiple constrained devices. The GPT2-903 <sup>904</sup> Large model in setting B with a memory reduction of 66.20% 905 shows a relatively minor performance decline in terms of 906 accuracy for datasets like ARC-c, WinoGrande, and BoolQ. <sup>907</sup> Here, ARC-e task shows the highest accuracy sensitivity to <sup>908</sup> memory reduction, i.e., a decrease of 23.28% in accuracy. <sup>909</sup> However, it is important to note that our DSE methodology and 910 algorithm prioritize the optimization for general PPL scores, <sup>911</sup> rather than tailoring the search to enhance specific task scores. 912 To further improve the accuracy of different datasets, our 913 DSE method can be applied to search for optimal design 914 points targeting the accuracy separately for each dataset. This approach allows for maintaining robust performance 915 916 while ensuring minimal accuracy drop for individual datasets. 917 However, it is important to recognize that this will result in 918 different optimal design points (different sets of R values) for 919 each dataset.

Overall, both models demonstrate a notable degree of 920 performance resilience under extreme failure scenarios, indicating their potential for effective deployment in environments 922 with memory constraints, such as edge devices. 923

924

## D. Robustness Verification Against Varying Failures

To deepen our understanding of *EASTER*'s robustness, we  $_{925}$  compare our robustness-aware method against the LP-inspired  $_{926}$  method which does not utilize the notion of the importance of  $_{927}$  neurons. To maintain a fair comparison, we select the settings  $_{928}$  marked as A–C in Fig. 6 to split the transformer models across  $_{929}$  four devices according to the *R* values associated with the  $_{930}$  three marked settings by utilizing the two methods.  $_{931}$ 

As depicted in Fig. 7, the *x*-axis categorizes the failure <sup>932</sup> scenarios (1D-Fail, 2-D-Fail, or 3D-Fail), whereas the *y*-axis <sup>933</sup> quantifies model performance, measured by the Top-1 accuracy on the ImageNet-1k validation dataset or perplexity (PPL) <sup>935</sup> value. Please note the logarithmic scale for the PPL scores. <sup>936</sup> The graphical representation uses blue bars to indicate the <sup>937</sup> performance of the traditional layer-wise partitioning (LPinspired) method in the face of device failures, while orange <sup>939</sup> bars illustrate the performance of our *EASTER* method. <sup>940</sup>

Consider Fig. 7(a) and the 2D-Fail scenario. When the 941 ViT-16 model is split with R = 0.33, the Top-1 error of 942 the LP-inspired method is as high as 94.742%, in contrast 943 to our method, which significantly lowers the Top-1 error to 944 54.626%. By increasing the *R* value from 0.33 to 0.53, we 945 observe a further reduction of the Top-1 error to 31.238%. 946 Increasing the *R* value further to 0.77 results in the Top-1 error 947 dropping to 20.614%, which is very close to the baseline Top-948 1 error of 18.572%. Note that our method can achieve this 949 baseline error if we set *R* to 1.0 (as shown in Fig. 7) because 950 this setting "forces" our method to perform full replication of 951 neurons, i.e., no accuracy loss is encountered due to device 952



Fig. 7. Robustness comparison of EASTER with layer-wise partitioning [7] across four devices. (a) ViT-16. (b) GPT2-Large. (c) Vicuna-7B.



Fig. 8. Inference latency, communication time, and memory usage for different models across device configurations. (a) ViT-16. (b) GPT2-Large. (c) Vicuna-7B.

<sup>953</sup> failures. Similarly, with the Vicuna7B model, the logarithmic <sup>954</sup> value of perplexity (PPL) observed using the LP-inspired <sup>955</sup> method under a 2D-Fail condition is 8.29. In contrast, our <sup>956</sup> method achieves a log(PPL) of 5.50 with an *R* value of 0.34. <sup>957</sup> Further increasing the R value to 0.76 results in an even lower <sup>958</sup> log(PPL) which is very close to the baseline (R = 1.0).

These results clearly demonstrate that our *EASTER* method significantly outperforms the LP-inspired method in maintaining model performance against device failures. Moreover, increasing the *R* value, which dictates the degree of neuron replication, can further improve model robustness.

# 964 E. Distributed Inference

In this section, we evaluate our end-to-end tool that facil-965 <sup>966</sup> itates automated model partitioning and its deployment on distributed edge devices. Our tool is specifically implemented 967 to convert standard PyTorch transformer models into optimized 968 multinode implementations following our EASTER method-969 970 ology, making the models suitable for efficient distributed 971 deployment on edge devices. We present empirical results, <sup>972</sup> obtained by using our edge test-bed described in Section VI-A, order to demonstrate the advantages of EASTER in terms 973 in overall end-to-end inference latency and maximum memory 974 Of 975 usage per device in a distributed system running transformer 976 models. Here, in all experiments, transformer blocks are evenly distributed across the devices. In Fig. 8, the light blue 977  $_{978}$  bars represent the computation time  $T_{cal}$  of the distributed 979 inference process, the gray blue bars indicate the communica- $_{360}$  tion/synchronization overhead  $T_{\rm comm}$ , whereas the orange bars <sup>981</sup> in Fig. 8 denote the maximum memory usage per device. The data is presented for different numbers of collaborating edge 982 devices across the three models. 983

As shown in Fig. 8, in most cases, the overall end-to- 984 end inference latency improves when increasing the number 985 of edge devices. As the number of devices increases, in 986 all cases, computation time  $T_{cal}$  (light blue bars) reduces 987 correspondingly. Only in the case of ViT-16 [Fig. 8(a)], this 988 advantage is counterbalanced by a rise in the communica- 989 tion overhead (gray bars), which, in an eight-device setup, 990 surpasses the computational savings, leading to an overall 991 increase in the inference latency. Conversely, for GPT2-Large, 992 the communication overhead, while increasing with more 993 devices, still remains a smaller fraction compared to the 994 computation time. This results in a near-linear acceleration, 995 with an overall inference latency decrease from 58.00 s using 996 one device to 7.62 s using eight devices. The increase in 997 communication overhead therefore seems more pronounced in 998 smaller transformer models like ViT-16, that represents a fun- 999 damental tradeoff between computation and communication. 1000

The results shown in Fig. 8 clearly indicate that with an 1001 increasing number of devices (from 1 to 8 devices), there 1002 also is a noticeable decrease in memory usage per device. For 1003 instance, the maximum on-device memory usage for ViT-16 1004 decreases from 193.8 MB in a single-device configuration to 1005 48.1 MB in an eight-device configuration. Similarly, GPT2- 1006 Large exhibits a significant memory reduction from 3.6 GB on 1007 a single device to 556.3 MB across eight devices. A significant 1008 reduction in memory usage per device from 27.6 GB on 1009 a single-device configuration to 4.6 GB on an eight-device 1010 configuration is observed for Vicuna-7B as shown in Fig. 8(c). 1011 Such reduction enables the models to run the complete float32 1012 1013 version at the edge without the need for extra swap space 1014 or model quantization, highlighting EASTER's effectiveness in 1015 memory savings.

Finally, if the reduction in computation time due to 1016 1017 distributed inference is outweighed by the increase in com-1018 munication time, the overall end-to-end latency increases. We can adjust timeout thresholds in the system to manage the 1019 tradeoff between computation and communication times. By 1020 implementing such a timeout mechanism, we ensure that if 1021 1022 synchronization among distributed devices does not conclude within the set time period, the system proceeds without further 1023 1024 delay, thus maintaining timely execution. This approach not 1025 only mitigates potential increases in communication time but 1026 also safeguards against the detrimental effects of prolonged 1027 synchronization wait times.

The above findings validate the efficiency of EASTER in 1028 1029 optimizing memory usage per device in distributed transformer <sup>1030</sup> inference, particularly in edge computing environments where <sup>1031</sup> resource constraints are a critical factor.

# VII. CONCLUSION

This article introduces EASTER, a novel method designed 1033 to robustly partition transformer models across edge devices, 1034 <sup>1035</sup> effectively addressing the challenge of potential device failures 1036 at the Edge. The EASTER method navigates the vast design 1037 space of splitting strategies by learning the expectation of different design subspaces. It also outperforms traditional 1038 state-of-the-art DSE methods in searching efficiency for 1039 1040 our distribution problem. Through extensive experimentation, EASTER has been proven to identify Pareto solutions within 1041 1042 a limited number of experimental trials efficiently.

Utilizing our developed end-to-end tool, we have the capa-1043 1044 bility to evaluate the distributed implementation on actual 1045 hardware boards, which allows us to confirm the advantages in 1046 memory usage and inference latency that distributed inference <sup>1047</sup> brings. Moreover, our findings substantiate that partial splitting significantly enhances model robustness in the face of device 1048 1049 failures. This approach not only minimizes memory consumption on each device but also has the potential to reduce 1050 overall end-to-end latency, presenting a valuable opportunity 1051 1052 for deploying large-scale transformer models within edge 1053 computing environments.

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