

2.80 $W = 500 \text{ N}$ $m = \frac{W}{g} = \frac{500}{9.81} = 50.97 \text{ kg}$

in b) $x_0 - x_1 = x_1 - x_2 = 2 \text{ mm} \Rightarrow$ Coulomb since linear decrement

a) $x_0 - x_1 = 4 \neq x_1 - x_2 = 2 \Rightarrow$ viscous since $\frac{x_0}{x_1} = 2 = \frac{x_1}{x_2} \Rightarrow$ log decrement
for a) $\delta = \ln \frac{x_0}{x_1} = \ln 2 = 0.6931 = \frac{2\pi\zeta}{\sqrt{1-\zeta^2}} \Rightarrow \zeta = \frac{\delta}{\sqrt{4\pi^2 + \delta^2}}$ or $\zeta \approx \frac{\delta}{2\pi} = .1096$

now for b) $\tau_n = 0.2 \text{ sec}$, $f_n = \frac{1}{\tau_n} = 5$ $\omega_n = 2\pi f_n = 31.42 \text{ rad/s}$

a) $\tau_d = 0.2 \text{ sec}$ $f_d = \frac{1}{\tau_d} = 5$ $\omega_d = 2\pi f_d = 31.42 \text{ rad/s}$; $\omega_d = \omega_n \sqrt{1-\zeta^2} \Rightarrow \omega_n = \frac{\omega_d}{\sqrt{1-\zeta^2}} = 31.61 \text{ rad/s}$

now for a) $k = m\omega_n^2 = 50.97 (31.61)^2 = 50929 \frac{\text{N}}{\text{m}}$

b) $k = m\omega_n^2 = 50.97 (31.42)^2 = 50,319 \text{ N/m}$

for a) $\omega_n = 31.61 \text{ rad/s}$ $\omega_d = 31.42 \text{ rad/s}$

b) $\omega_n = \omega_d = 31.42 \text{ rad/s}$

to determine what the friction value is

for a) since viscous damping ζ is damping ratio $c_{crit} = 2m\omega_n = 2(50.97)(31.61) = 3222.3 \text{ N-s/m}$

$\zeta/c_{crit} = \zeta \Rightarrow c = \zeta \cdot c_{crit} = .1096(3222.3) = 353.2 \frac{\text{N-s}}{\text{m}}$

for b) $x_0 - x_1 = 2 \text{ mm} = .002 \text{ m} = 4 f_{1c}$ $\therefore f = \frac{.002 \text{ k}}{4} = \frac{.002(50319)}{4} = 25.16 \text{ N} = \mu W$

$\therefore \mu = f/W = \frac{25.16}{500} = .0503$