## Instructor's Solutions Manual

ENGINEERING MECHANICS

# DYNAMICS

TWELFTH EDITION

R. C. HIBBELER

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### CONTENTS

To the Instructor	
12 General Principles	1
13 Force Vectors	177
14 Equilibrium of a Particle	285
15 Force System Resultants	355
16 Equilibrium of a Rigid Body	513
17 Structural Analysis	641
18 Internal Forces	725
19 Friction	779
20 Center of Gravity and Centroid	867
21 Moments of Inertia	925
22 Virtual Work	988

#### To the Instructor

This manual contains the solutions to all the problems in *Engineering Mechanics: Dynamics, Twelfth Edition*. As stated in the preface of the text, the problems in every section are arranged in an approximate order of increasing difficulty. Be aware that answers to all but every fourth problem, which is indicated by an asterisk (\*), are listed in the back of the book. Also, every fourth problem has an additional hint for the solution and is indicated with a bullet (•). Finally, those problems indicated by a square ( $\blacksquare$ ) will require additional numerical work.

You may wish to use one of the lists of homework problems given on the following pages. Here you will find four lists for which the answers are in the back of the book, a fifth list for problems without answers, and a sixth sheet which can be used to develop your own personal syllabus. The prepared lists generally represent assignments with an easy, a moderate, and sometimes a more challenging problem.

If you have any questions regarding the solutions in this manual, I would greatly appreciate hearing from you.

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Section	Title	Assignment with Hints and Answers
12.1–12.2	Rectilinear Motion	12-8, 12-12, 12-20, 12-32
12.3	Graphical Solutions	12-52, 12-48, 12-60
12.4–12.6	Curvilinear x, y, z Motion	12-72, 12-76, 12-96, 12-104
12.7	Curvilinear <i>n</i> , <i>t</i> , <i>b</i> Motion	12–112, 12–124, 12–144
12.8	Curvilinear $r, \theta, z$ Motion	12-156, 12-164, 12-180
12.9	Dependent Motion	12-196, 12-204, 12-208
12.10	Independent Motion	12-224, 12-216, 12-220
13.1–13.4	Equation of Motion <i>x</i> , <i>y</i> , <i>z</i>	13-16, 13-12, 13-24, 13-32
13.5	Equation of Motion <i>n</i> , <i>t</i> , <i>b</i>	13-52, 13-68, 13-72
13.6	Equation of Motion $r, \theta, z$	13-92, 13-96, 13-108
13.7	Space Mechanics	13-120, 13-124, 13-136
14.1–14.3	Principle of Work and Energy	14-4, 14-12, 14-20
14.4	Power and Efficiency	14-48, 14-52, 14-64
14.5–14.6	Conservation of Energy	14-80, 14-54, 14-96
15.1	Linear Momentum	15-8, 15-16, 15-28
15.2–15.3	Conservation of Linear Momentum	15-32, 15-40, 15-48
15.4	Impact	15-60, 15-64, 15-84
15.5	Angular Momentum	15-96, 15-100, 15-104
*15.8	Steady Fluid Flow	15–112, 15–116, 15–120
*15.9	Variable Mass	15-108, 15-128, 15-136
16.1–16.3	Rotation About a Fixed Axis	16-12, 16-16, 16-24
16.4	Absolute Motion Analysis	16–36, 16–44, 16–48
16.5	Relative Velocity Analysis	16-56, 16-68, 16-80
16.6	Inst. Center of Zero Velocity	16-84, 16-92, 16-104
16.7	Relative Acceleration Analysis	16–116, 16–124, 16–128
16.8	Motion Using Rotating Axes	16–114, 16–148, 16–156
17.1	Moment of Inertia	17-8, 17-16, 17-20
17.2–17.3	Eq. of Motion-Translation	17–32, 17–40, 17–48
17.4	Eq. of Motion-Fixed Axis Rotation	17–64, 17–72, 17–88
17.5	Eq. of Motion-Gen. Plane Motion	17–96, 17–104, 17–108
18.1–18.4	Principle of Work and Energy	18-8, 18-20, 18-28
18.5	Conservation of Energy	18-44, 18-56, 18-64
19.1–19.2	Principle of Impulse and Momentum	19–8, 19–16, 19–20
19.3	Cons. of Angular Momentum	19–36, 19–40, 19–44
19.4	Eccentric Impact	19–52, 19–56
*20.1-*20.2	Rotation About a Fixed Point	20-4, 20-12, 20-16
*20.3	General Motion	20–24, 20–28, 20–32
*20.4	Relative Motion Analysis	20-40, 20-44, 20-52
*21.1	Moment of Inertia	21-8, 21-12, 21-16
*21.2-*21.3	Imp. and Mom., Work and Energy	21–28, 21–32, 21–36
*21.4	Euler Equations of Motion	21-44, 21-52, 21-56
*21.5-*21.6	Gyroscopic and Torque Free Motion	21-64, 21-68, 21-72
22.1	Free Vibration	22-4, 22-8, 22-20
22.2	Energy Methods	22–32, 22–36, 22–40
*22.3-*22.4	Forced Vib., Damped Free Vib.	22-44, 22-52, 22-72
*22.5-*22.6	Damped Forced Vib., Elec. Analog	22-64, 22-68, 22-76

Section	Торіс	Assignment List 1 with Answers
12.1–12.2	Rectilinear Motion	12-2, 12-7, 12-30
12.3	Graphical Solutions	12-46, 12-51, 12-55
12.4–12.6	Curvilinear <i>x</i> , <i>y</i> , <i>z</i> Motion	12-71, 12-75, 12-95, 12-109
12.7	Curvilinear <i>n</i> , <i>t</i> , <i>b</i> Motion	12-118, 12-125, 12-131
12.8	Curvilinear $r, \theta, z$ Motion	12-162, 12-166, 12-177
12.9	Dependent Motion	12-203, 12-210, 12-214
12.10	Independent Motion	12-226, 12-227, 12-229
13.1–13.4	Equation of Motion <i>x</i> , <i>y</i> , <i>z</i>	13-10, 13-19, 13-26
13.5	Equation of Motion <i>n</i> , <i>t</i> , <i>b</i>	13-51, 13-67, 13-75
13.6	Equation of Motion $r, \theta, z$	13-85, 13-95, 13-106
13.7	Space Mechanics	13–118, 13–126, 13–131
14.1–14.3	Principle of Work and Energy	14-3, 14-19, 14-23
14.4	Power and Efficiency	14-46, 14-61, 14-70
14.5–14.6	Conservation of Energy	14-79, 14-90, 14-102
15.1	Linear Momentum	15-7, 15-19, 15-27
15.2–15.3	Conservation of Linear Momentum	15-37, 15-43, 15-46
15.4	Impact	15-66, 15-79, 15-86
15.5	Angular Momentum	15-90, 15-94, 15-101
*15.8	Steady Fluid Flow	15–115, 15–118, 15–121
*15.9	Variable Mass	15-127, 15-131, 15-139
16.1–16.3	Rotation About a Fixed Axis	16-10, 16-15, 16-26
16.4	Absolute Motion Analysis	16-39, 16-41, 16-50
16.5	Relative Velocity Analysis	16-59, 16-67, 16-73
16.6	Inst. Center of Zero Velocity	16–94, 16–98, 16–105
16.7	Relative Acceleration Analysis	16–109, 16–118, 16–133
16.8	Motion Using Rotating Axes	16-138, 16-141, 16-158
17.1	Moment of Inertia	17-5, 17-15, 17-19
17.2–17.3	Eq. of Motion-Translation	17–33, 17–38, 17–45
17.4	Eq. of Motion-Fixed Axis Rotation	17-67, 17-74, 17-86
17.5	Eq. of Motion-Gen. Plane Motion	17–107, 17–113, 17–121
18.1–18.4	Principle of Work and Energy	18–2, 18–23, 18–34
18.5	Conservation of Energy	18-42, 18-50, 18-65
19.1–19.2	Principle of Impulse and Momentum	19–9, 19–14, 19–29
19.3	Cons. of Angular Momentum	19–34, 19–38, 19–47
19.4	Eccentric Impact	19-46, 19-51, 19-55
*20.1-*20.2	Rotation About a Fixed Point	20-11, 20-15, 20-19
*20.3	General Motion	20-22, 20-30, 20-34
*20.4	Relative Motion Analysis	20-46, 20-50, 20-55
*21.1	Moment of Inertia	21-9, 21-18, 21-19
*21.2-*21.3	Imp. and Mom., Work and Energy	21-27, 21-31, 21-39
*21.4	Euler Equations of Motion	21-51, 21-54, 21-58
*21.5-*21.6	Gyroscopic and Torque Free Motion	21-65, 21-66, 21-77, 21-78
22.1	Free Vibration	22-6, 22-14, 22-19
22.2	Energy Methods	22–29, 22–31, 22–37
*22.3-*22.4	Forced Vib., Damped Free Vib.	22-50, 22-53, 22-54
*22.5-*22.6	Damped Forced Vib., Elec. Analog	22-69, 22-71, 22-74

Section	Торіс	Assignment List 2 with Answers
12.1-2	Rectilinear Motion	12-5, 12-17, 12-25
12.3	Graphical Solutions	12-45, 12-57, 12-65
12.4–12.6	Curvilinear <i>x</i> , <i>y</i> , <i>z</i> Motion	12-73, 12-77, 12-81, 12-101, 12-105
12.7	Curvilinear <i>n</i> , <i>t</i> , <i>b</i> Motion	12-113, 12-121, 12-129
12.8	Curvilinear $r, \theta, z$ Motion	12-157, 12-165, 12-181
12.9	Dependent Motion	12-197, 12-205, 12-213
12.10	Independent Motion	12-217, 12-221, 12-225
13.1–13.4	Equation of Motion <i>x</i> , <i>y</i> , <i>z</i>	13-5, 13-13, 13-25
13.5	Equation of Motion <i>n</i> , <i>t</i> , <i>b</i>	13-49, 13-58, 13-73
13.6	Equation of Motion $r, \theta, z$	13-93, 13-109, 13-113
13.7	Space Mechanics	13-125, 13-129, 13-137
14.1–14.3	Principle of Work and Energy	14-13, 14-21, 14-29
14.4	Power and Efficiency	14-45, 14-53, 14-65
14.5–14.6	Conservation of Energy	14-77, 14-89, 14-93
15.1	Linear Momentum	15-13, 15-21, 15-29
15.2–15.3	Conservation of Linear Momentum	15-33, 15-45, 15-53
15.4	Impact	15-61, 15-65, 15-81
15.5	Angular Momentum	15-93, 15-97, 15-105
*15.8	Steady Fluid Flow	15-113, 15-117, 15-121
*15.9	Variable Mass	15-109, 15-129, 15-137
16.1–16.3	Rotation About a Fixed Axis	16-9, 16-17, 16-25
16.4	Absolute Motion Analysis	16-37, 16-45, 16-49
16.5	Relative Velocity Analysis	16-57, 16-65, 16-69
16.6	Inst. Center of Zero Velocity	16-85, 16-89, 16-93
16.7	Relative Acceleration Analysis	16-113, 16-121, 16-129
16.8	Motion Using Rotating Axes	16–137, 16–149, 16–157
17.1	Moment of Inertia	17-9, 17-13, 17-21
17.2–17.3	Eq. of Motion-Translation	17-34, 17-41, 17-49
17.4	Eq. of Motion-Fixed Axis Rotation	17-61, 17-65, 17-85
17.5	Eq. of Motion-Gen. Plane Motion	17–97, 17–105, 17–109
18.1–18.4	Principle of Work and Energy	18–9, 18–17, 18–29
18.5	Conservation of Energy	18-41, 18-45, 18-61
19.1–19.2	Principle of Impulse and Momentum	19–5, 19–13, 19–21
19.3	Cons. of Angular Momentum	19-33, 19-37, 19-41
19.4	Eccentric Impact	19-45, 19-49, 19-53
*20.1-*20.2	Rotation About a Fixed Point	20-5, 20-9, 20-13
*20.3	General Motion	20-29, 20-33, 20-37
*20.4	Relative Motion Analysis	20-45, 20-49, 20-53
*21.1	Moment of Inertia	21-9, 21-13, 21-17
*21.2-*21.3	Imp. and Mom., Work and Energy	21-25, 21-29, 21-33
*21.4	Euler Equations of Motion	21-49, 21-53, 21-57
*21.5-*21.6	Gyroscopic and Torque Free Motion	21-65, 21-73, 21-81
22.1	Free Vibration	22-5, 22-17, 22-21
22.2	Energy Methods	22–33, 22–37, 22–41
*22.3-*22.4	Forced Vib., Damped Free Vib.	22-45, 22-49, 22-53
*22.5-*22.6	Damped Forced Vib., Elec. Analog	22-61, 22-65, 22-69

Section	Торіс	Assignment List 3 with Answers
12.1–12.2	Rectilinear Motion	12-14, 12-19, 12-23
12.3	Graphical Solutions	12-43, 12-50, 12-58
12.4–12.6	Curvilinear <i>x</i> , <i>y</i> , <i>z</i> Motion	12-74, 12-83, 12-90, 12-103, 12-106
12.7	Curvilinear <i>n</i> , <i>t</i> , <i>b</i> Motion	12–14, 12–22, 12–26
12.8	Curvilinear $r, \theta, z$ Motion	12-159, 12-170, 12-178
12.9	Dependent Motion	12-21, 12-199, 12-206
12.10	Independent Motion	12–218, 12–223, 12–231
13.1–13.4	Equation of Motion <i>x</i> , <i>y</i> , <i>z</i>	13-22, 13-31, 13-38
13.5	Equation of Motion <i>n</i> , <i>t</i> , <i>b</i>	13-66, 13-70, 13-77
13.6	Equation of Motion $r, \theta, z$	13-94, 13-102, 13-110
13.7	Space Mechanics	13–122, 13–127, 13–133
14.1–14.3	Principle of Work and Energy	14-15, 14-22, 14-30
14.4	Power and Efficiency	14-50, 14-62, 14-67
14.5–14.6	Conservation of Energy	14-74, 14-86, 14-91
15.1	Linear Momentum	15-10, 15-18, 15-26
15.2–15.3	Conservation of Linear Momentum	15-39, 15-47, 15-51
15.4	Impact	15-63, 15-75, 15-53
15.5	Angular Momentum	15-95, 15-99, 15-102
*15.8	Steady Fluid Flow	15–111, 15–114, 15–119
*15.9	Variable Mass	15-126, 15-133, 15-138
16.1–16.3	Rotation About a Fixed Axis	16-6, 16-14, 16-31
16.4	Absolute Motion Analysis	16-42, 16-43, 16-51
16.5	Relative Velocity Analysis	16-58, 16-70, 16-78
16.6	Inst. Center of Zero Velocity	16-83, 16-90, 16-95
16.7	Relative Acceleration Analysis	16–114, 16–122, 16–127
16.8	Motion Using Rotating Axes	16–139, 16–142, 16–154
17.1	Moment of Inertia	17-1, 17-11, 17-23
17.2–17.3	Eq. of Motion-Translation	17-27, 17-35, 17-47
17.4	Eq. of Motion-Fixed Axis Rotation	17-62, 17-70, 17-82
17.5	Eq. of Motion-Gen. Plane Motion	17–99, 17–110, 17–119
18.1–18.4	Principle of Work and Energy	18-3, 18-15, 18-22
18.5	Conservation of Energy	18-38, 18-47, 18-55
19.1–19.2	Principle of Impulse and Momentum	19–10, 19–19, 19–23
19.3	Cons. of Angular Momentum	19-34, 19-35, 19-39
19.4	Eccentric Impact	19-50, 19-51, 19-55
*20.1-*20.2	Rotation About a Fixed Point	20-6, 20-7, 20-10
*20.3	General Motion	20-26, 20-30, 20-38
*20.4	Relative Motion Analysis	20-39, 20-46, 20-51
*21.1	Moment of Inertia	21-2, 21-7, 21-15
*21.2-*21.3	Imp. and Mom., Work and Energy	21-22, 21-26, 21-34
*21.4	Euler Equations of Motion	21-43, 21-50, 21-58
*21.5-*21.6	Gyroscopic and Torque Free Motion	21-62, 21-66, 21-71
22.1	Free Vibration	22-1, 22-10, 22-23
22.2	Energy Methods	22-30, 22-34, 22-39
*22.3-*22.4	Forced Vib., Damped Free Vib.	22-42, 22-50, 22-51
*22.5-*22.6	Damped Forced Vib., Elec. Analog	22-62, 22-74, 22-75

Section	Торіс	Assignment List 3
12.1–12.2	Rectilinear Motion	12-15, 12-18, 12-26
12.3	Graphical Solutions	12-42, 12-62, 12-67
12.4–12.6	Curvilinear x, y, z Motion	12-82, 12-86, 12-102
12.7	Curvilinear <i>n</i> , <i>t</i> , <i>b</i> Motion	12-111, 12-123, 12-130
12.8	Curvilinear $r, \theta, z$ Motion	12-158, 12-174, 12-187
12.9	Dependent Motion	12-195, 12-202, 12-207
12.10	Independent Motion	12-215, 12-219, 12-222
13.1–13.4	Equation of Motion <i>x</i> , <i>y</i> , <i>z</i>	13-7, 13-18, 13-23
13.5	Equation of Motion <i>n</i> , <i>t</i> , <i>b</i>	13-50, 13-63, 13-71
13.6	Equation of Motion $r, \theta, z$	13-86, 13-91, 13-105
13.7	Space Mechanics	13-117, 13-123, 13-130
14.1–14.3	Principle of Work and Energy	14-2, 14-10, 14-26
14.4	Power and Efficiency	14-43, 14-54, 14-66
14.5–14.6	Conservation of Energy	14-75, 14-83, 14-97
15.1	Linear Momentum	15-2, 15-15, 15-23
15.2–15.3	Conservation of Linear Momentum	15-34, 15-38, 15-50
15.4	Impact	15-62, 15-70, 15-78
15.5	Angular Momentum	15-91, 15-95, 15-103
*15.8	Steady Fluid Flow	15–111, 15–118, 15–122
*15.9	Variable Mass	15-123, 15-130, 15-135
16.1–16.3	Rotation About a Fixed Axis	16-3, 16-22, 16-26
16.4	Absolute Motion Analysis	16–38, 16–47, 16–53
16.5	Relative Velocity Analysis	16-55, 16-66, 16-74
16.6	Inst. Center of Zero Velocity	16-82, 16-87, 16-91
16.7	Relative Acceleration Analysis	16–111, 16–115, 16–123
16.8	Motion Using Rotating Axes	16–135, 16–146, 16–155
17.1	Moment of Inertia	17–3, 17–10, 17–18
17.2–17.3	Eq. of Motion-Translation	17–28, 17–31, 17–37
17.4	Eq. of Motion-Fixed Axis Rotation	17–59, 17–71, 17–83
17.5	Eq. of Motion-Gen. Plane Motion	17–98, 17–106, 17–115
18.1–18.4	Principle of Work and Energy	18-11, 18-14, 18-26
18.5	Conservation of Energy	18–35, 18–46, 18–54
19.1–19.2	Principle of Impulse and Momentum	19–7, 19–15, 19–22
19.3	Cons. of Angular Momentum	19–34, 19–38, 19–42
19.4	Eccentric Impact	19–47, 19–54, 19–55
*20.1-*20.2	Rotation About a Fixed Point	20-2, 20-3, 20-14
*20.3	General Motion	20-27, 20-31, 20-35
*20.4	Relative Motion Analysis	20-43, 20-47, 20-54
*21.1	Moment of Inertia	21-10, 21-11, 21-14
*21.2-*21.3	Imp. and Mom., Work and Energy	21-23, 21-32, 21-35
*21.4	Euler Equations of Motion	21-46, 21-55, 21-59
*21.5-*21.6	Gyroscopic and Torque Free Motion	21-63, 21-67, 21-75, 21-79
22.1	Free Vibration	22–2, 22–15, 22–18
22.2	Energy Methods	22-28, 22-35, 22-38
*22.3-*22.4	Forced Vib., Damped Free Vib.	22-43, 22-46, 22-58
*22.5-*22.6	Damped Forced Vib., Elec. Analog	22-63, 22-66, 22-71

Section	Торіс	Assignment
12.1–12.2	Rectilinear Motion	
12.3	Graphical Solutions	
12.4–12.6	Curvilinear x, y, z Motion	
12.7	Curvilinear <i>n</i> , <i>t</i> , <i>b</i> Motion	
12.8	Curvilinear $r, \theta, z$ Motion	
12.9	Dependent Motion	
12.10	Independent Motion	
13.1–13.4	Equation of Motion <i>x</i> , <i>y</i> , <i>z</i>	
13.5	Equation of Motion <i>n</i> , <i>t</i> , <i>b</i>	
13.6	Equation of Motion $r, \theta, z$	
13.7	Space Mechanics	
14.1–14.3	Principle of Work and Energy	
14.4	Power and Efficiency	
14.5–14.6	Conservation of Energy	
15.1	Linear Momentum	
15.2–15.3	Conservation of Linear Momentum	
15.4	Impact	
15.5	Angular Momentum	
*15.8	Steady Fluid Flow	
*15.9	Variable Mass	
16.1–16.3	Rotation About a Fixed Axis	
16.4	Absolute Motion Analysis	
16.5	Relative Velocity Analysis	
16.6	Inst. Center of Zero Velocity	
16.7	Relative Acceleration Analysis	
16.8	Motion Using Rotating Axes	
17.1	Moment of Inertia	
17.2–17.3	Eq. of Motion-Translation	
17.4	Eq. of Motion-Fixed Axis Rotation	
17.5	Eq. of Motion-Gen. Plane Motion	
18.1–18.4	Principle of Work and Energy	
18.5	Conservation of Energy	
19.1–19.2	Principle of Impulse and Momentum	
19.3	Cons. of Angular Momentum	
19.4	Eccentric Impact	
*20.1-*20.2	Rotation About a Fixed Point	
*20.3	General Motion	
*20.4	Relative Motion Analysis	
*21.1	Moment of Inertia	
*21.2-*21.3	Imp. and Mom., Work and Energy	
*21.4	Euler Equations of Motion	
*21.5-*21.6	Gyroscopic and Torque Free Motion	
22.1	Free Vibration	
22.2	Energy Methods	
*22.3-*22.4	Forced Vib., Damped Free Vib.	
*22.5-*22.6	Damped Forced Vib., Elec. Analog	