

$$\frac{\partial}{\partial y} (\bar{P} \bar{t} \frac{\partial w}{\partial y}) + \frac{\partial}{\partial x} (\bar{P} \bar{t} \frac{\partial w}{\partial x}) + f(x, y, t) = \rho \frac{\partial^2 w}{\partial t^2} \bar{t}$$

IF $\bar{t} = \text{const}$ $\frac{\partial}{\partial y} (\bar{P} \frac{\partial w}{\partial y}) + \frac{\partial}{\partial x} (\bar{P} \frac{\partial w}{\partial x}) + f/\bar{t} = \rho w_{tt}$

IF $\bar{P}$ is constant $\Rightarrow w_{xx} + w_{yy} + f/\bar{t}\bar{P} = \rho/\bar{P} w_{tt}$

IF $f=0 \Rightarrow w_{xx} + w_{yy} = \frac{1}{c^2} w_{tt}$ and $\nabla^2 w = \frac{1}{c^2} w_{tt}$ $c = \sqrt{\frac{\bar{P}}{\rho}}$

• IF steady state $\frac{\partial}{\partial t} = 0 \Rightarrow \nabla^2 w = 0$ Elliptic eqn.

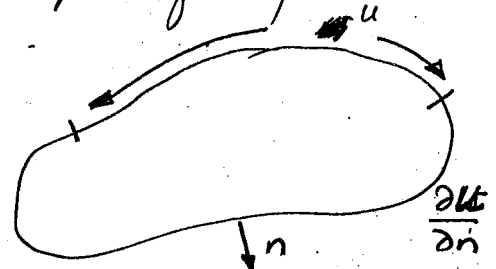
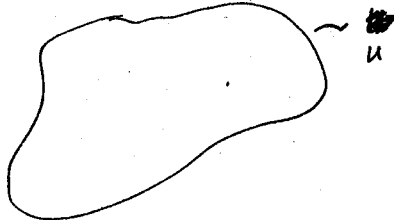
• Boundary Conditions + initial conditions IN GENERAL

• for each time derivative you need 1 initial condition

• for each space derivative $\frac{\partial}{\partial x}, \frac{\partial}{\partial y}$ you need 1 boundary condition

• FOR ELLIPTIC TYPE EQNS need to specify value on bdy, or deriv on bdy, or value normal, or ∇u and derivative on different parts of bdy

must also satisfy consistency of Neumann
 $\int \frac{\partial u}{\partial n} ds = \iint \nabla^2 u dA$
 using Divergence theorem.



• FOR PARABOLIC TYPE - heat eqn $u_{xx} = a u_t$

• need 1 initial condition $u(x, t=t_0) = u_0(x)$

• need value or value + deriv on boundary: $\alpha u + \beta u_n$

• FOR HYPERBOLIC - wave eqn

• need 2 initial conditions $u(x, t=t_0) = u_0(x)$
 $\frac{\partial u}{\partial t}(x, t=t_0) = u_1(x)$

• need value or value + deriv on boundary