# Probability and Extreme Floods 

CWR 5305 - Surface Hydrology

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## Background

- Floods and droughts are extreme hydrological events.
- If available, streamflow and/or precipitation records are the basis to estimate floods and droughts:
- When records are not long enough, extrapolation and statistical techniques are used to "estimate" extreme values
- If not available, empirical and other methods are also used to estimate extreme values


## Recurrence Interval or Return Period, T, and Probability of Occurrence

- Floods (in high-flow analysis) will be equal or exceeded in a period of time (i.e., T )
$-T=1 / P_{z}$, where $P=$ probability of occurrence
- Droughts (in low-flow analysis) will be equaled or less:
$-T=1 / P_{\leq}$, where $P=$ probability of occurrence


## Methods for Extreme (Flood) Flow \& Drought Computation

Figure 11.1 Methods for flood flow computation and procedures used in drought analysis.


## Basic Definitions

- Discrete versus continuous random variables (e.g., floods, droughts, precipitation measurements, infiltration rates, etc.)
- Variate = individual observation or value (e.g., a discharge of $1 \mathrm{ft}^{3} / \mathrm{s}$ measured at a particular location at a specific time)
- Time series = an array of variates
- Classes = equal intervals of groups of variates (e.g., 0-$10,10-20,20-30,30-40, \ldots, \mathrm{ft}^{3} / \mathrm{s}$ )
- Frequency = number of items (or variates) in a class


## Frequency Distribution Curve:

$n_{i}=$ number of items in ith-class; $N=$ total number of items in a series

$$
p=n_{i} / N \text { [Eq. 11.1] }
$$

Figure 11.2 Frequency distribution curve.


## Probability Distributions

- For continuous random variable, $x$ :
- PDF or Probability Density Function
- CPD or Cumulative Distribution Function
- Common PDFs (See 11.5 for detailed list with properties):
- Normal,
- Lognormal
- Extreme value
- Log-Pearson Type III (Gamma Type)


## Common PDFs

## Table 11.5 Properties of Common Distributions

Probability Density Function Cumulative Density Function

$\Gamma$ is the gamma function; $\Gamma(n)=(n-1)$ !.
$\alpha$ and $\beta$ are evaluated from relations shown under the columns of mean and standard deviation.
$c$ and $\alpha$ are evaluated from relations shown under the columns of mean and standard deviation.

## Cumulative Probability Curve

Figure 11.3 Cumulative probability curve.


## Design Flood for Structures

- Acceptable Level of Risk:
- Probable Maximum Flood
- Optimum Design Flood for a Return Period, T
- Economic Factors:
- For instance, peak flow rate at a Return Period, T, that minimizes the average annual cost (construction cost, O\&M, damage cost)
- Standard Practice:
- Based on
- type of structure,
- importance of the structure, and
- development of the area subject to flooding


## Probability of at Least One Flood in $n$-years

- $\mathrm{f}_{\mathrm{x}}($ exactly k events in n years $)=$ $C_{k}^{n} P^{k}(1-P)^{n-k}$
- $f_{x}$ (at least one flood in $n$ years) $=$ $1-(1-P)^{n}$, where $P_{z}=1 / T$
- Risk $=R=f_{x} \times 100$


## Risk level $=f($ Return Period)

Table 11.1 Return Period, 1/P, For Various Risk Levels [eq. (11.4)]

|  | Project Life, $n$ (years) |  |  |
| :---: | :---: | :---: | :---: |
| Acceptable Level of | 50 | 100 |  |
| Risk, | 25 | Return Period |  |
| $R(\%)$ | 2440 | 5260 | 9950 |
| 1 | 87 | 175 | 345 |
| 25 | 37 | 72 | 145 |
| 50 | 18 | 37 | 72 |
| 75 | 6 | 11 | 27 |

## Probability Paper

- General Purpose:
- To "linearize" the plot (i.e., $\mathrm{Y}=\mathrm{MX}+\mathrm{N}$ ) for different CDFs
- Probability paper for
- Normal
- Lognormal
- Type I extreme value or Gumbel
- Type III extreme value or Weibull


## Methods of Flood Frequency Analysis

- Graphical Method
- Usable for long records (not that common)
- Based on plotting of a Frequency Distribution Curve (see Figure 11.2) that is data organized by classes and their frequencies
- Common paper: lognormal probability
- Empirical Method
- Also graphical
- Based on a ranking of variates from largest to smallest to estimate P or T for a plotting position (see Example 11.5)
- Analytical Method
- Based on linearized functions, such as Equation 11.10, and the K-T relationships for each PDF of choice (see tables 11.6, 11.7 and 11.7)


## Graphical Method

- Just like the development of a "frequency distribution" curve/plot as illustrated in Figure 11.2 and examples.
- Procedure:
- Flood flows are arranged into several class intervals of equal range in discharge;
- Cumulate the number of occurrences in each class, starting with the highest value;
- Determine the \% of the class occurrences per total occurrences;
- Plot the \% versus the lower discharge limit of each class on probability paper (i.e., commonly lognormal probability paper)


## Example: Empirical Method:

$n_{i}=$ number of items in ith-class; $N=$ total number of items in a series

$$
p=n_{i} / N \text { [Eq. 11.1] }
$$

Figure 11.2 Frequency distribution curve.


## Empirical Method

- Also, a graphical method, as follows:
- Organize an array of $n$ flood flow values in descending order of magnitude starting with the highest value;
- Assign a rank $m$ to each value, 1 to $n$, form the highest to the smallest one;
- Calculate the "plotting position" using Weibull's formula (1939):
- $P_{m}=m /(n+1)$ or Equation 11.9, p. 436
- Plot flow (i.e., discharge) versus the plotting position (or percent probability of exceedance)on lognormal probability paper (see example of Figure 11.6)
- See application of Example 11.5.


## Example 11.5: Empirical Method

Table 11.4 Annual Peak Flows of the River in Example 11.5

| (1) | (2) | (3) | (4) <br> Ploting | (1) | (2) | (3) | $(4)$ <br> Position <br> (\%) |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Year | Flow (cfs) | Year | Flow (cfs) | Rank | Position <br> (\%) |  |  |
| 1991 | 14,400 | 5 | 20 | 2003 | 6,440 | 17 | 68 |
| 1992 | 6,720 | 16 | 64 | 2004 | 22,700 | 1 | 4 |
| 1993 | 13,390 | 7 | 28 | 2005 | 11,140 | 10 | 40 |
| 1994 | 15,360 | 4 | 16 | 2006 | 4,560 | 21 | 84 |
| 1995 | 8,856 | 13 | 52 | 2007 | 5,376 | 19 | 76 |
| 1996 | 5,136 | 20 | 80 | 2008 | 12,480 | 9 | 36 |
| 1997 | 6,770 | 15 | 60 | 2009 | 19,200 | 3 | 12 |
| 1998 | 9,600 | 12 | 48 | 2010 | 12,984 | 8 | 32 |
| 1999 | 980 | 24 | 96 | 2011 | 5,450 | 18 | 72 |
| 2000 | 4,030 | 22 | 88 | 2012 | 13,440 | 6 | 24 |
| 2001 | 10,440 | 11 | 44 | 2013 | 22,680 | 2 | 8 |
| 2002 | 3,100 | 23 | 92 | 2014 | 8,400 | 14 | 56 |

Figure 11.6 Flood-frequency curve for Example 11.5.


## Analytical Method Distributions

 (i.e., commonly used in hydrologic engineering)- Normal (Gaussian) Distribution
- Lognormal Distribution
- Extreme Value Distribution (or Gumbel)
- Log-Pearson Type III (Gamma-Type) Distribution - adopted as standard by U.S. federal agencies for flood analysis


## Analytical Method

- In classical analysis, the CDF is solved in tables that provide the cumulative (exceedance) probability for a desired flow value or
- In hydrological engineering, we used Chow simplified approach (1951), with $Y=\log X$
$-X=\ddot{X}+K S\left(L^{3} T^{-1}\right)$ for the Normal (Gaussian) distribution; $K=$ frequency factor of used PDF
$-\mathrm{Y}=\overline{\mathrm{Y}}+\mathrm{KS}\left(\mathrm{L}^{3} \mathrm{~T}^{-1}\right)$ for the Lognormal, Log-Pearson Type III (Gamma-type) and Type I extreme value (Gumbel) distributions; $K=$ frequency factor of used PDF
- See steps in Section 11.10.1 - Use of frequency factors


## K - Normal Probability Distribution

Table 11.6 Frequency Factor for Normal Distribution

| Exceedance Probability | Return Period | K | Exceedance Probability | Return Period | K |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 0.0001 | 10,000 | 3.719 | 0.450 | 2.22 | 0.126 |
| 0.0005 | 2,000 | 3.291 | 0.500 | 2.00 | 0.000 |
| 0.001 | 1,000 | 3.090 | 0.550 | 1.82 | -0.126 |
| 0.002 | 500 | 2.88 | 0.600 | 1.67 | -0.253 |
| 0.003 | 333 | 2.76 | 0.650 | 1.54 | -0.385 |
| 0.004 | 250 | 2.65 | 0.700 | 1.43 | -0.524 |
| 0.005 | 200 | 2.576 | 0.750 | 1.33 | -0.674 |
| 0.010 | 100 | 2.326 | 0.800 | 1.25 | -0.842 |
| 0.025 | 40 | 1.960 | 0.850 | 1.18 | -1.036 |
| 0.050 | 20 | 1.645 | 0.900 | 1.11 | -1.282 |
| 0.100 | 10 | 1.282 | 0.950 | 1.053 | -1.645 |
| 0.150 | 6.67 | 1.036 | 0.975 | 1.026 | -1.960 |
| 0.200 | 5.00 | 0.842 | 0.990 | 1.010 | -2.326 |
| 0.250 | 4.00 | 0.674 | 0.995 | 1.005 | -2.576 |
| 0.300 | 3.33 | 0.524 | 0.999 | 1.001 | -3.090 |
| 0.350 | 2.86 | 0.385 | 0.9995 | 1.0005 | -3.291 |
| 0.400 | 2.50 | 0.253 | 0.9999 | 1.0001 | -3.719 |

## K - Log-Pearson Type III Distribution

| Table 11.7 <br> Skew Coefficient, 9 | Probability |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | 0.99 | 0.80 | 0.50 |  | 0.10 | 0.04 | 0.02 | 0.01 |
|  | Return Period |  |  |  |  |  |  |  |
|  | 1.0101 | 1.2500 | 2 | 5 | 10 | 25 | 50 | 100 |
| 3.0 | -0.667 | -0.636 | -0.396 | 0.420 | 1.180 | 2.278 | 3.152 | 4.051 |
| 2.8 | -0.714 | -0.666 | -0.384 | 0.460 | 1.210 | 2.275 | 3.114 | 3.973 |
| 2.6 | -0.769 | -0.696 | -0.368 | 0.499 | 1.238 | 2.267 | 3.071 | 3.889 |
| 2.4 | -0.832 | -0.725 | $-0.351$ | 0.537 | 1.262 | 2.256 | 3.023 | 3.800 |
| 2.2 | -0.905 | -0.752 | -0.330 | 0.574 | 1.284 | 2.240 | 2.970 | 3.705 |
| 2.0 | -0.990 | -0.777 | $-0.307$ | 0.609 | 1.302 | 2.219 | 2.912 | 3.605 |
| 1.8 | -1.087 | -0.799 | $-0.282$ | 0.643 | 1.318 | 2.193 | 2.848 | 3.499 |
| 1.6 | -1.197 | -0.817 | -0.254 | 0.675 | 1.329 | 2.163 | 2.780 | 3.388 |
| 1.4 | $-1.318$ | $-0.832$ | -0.225 | 0.705 | 1.337 | 2.128 | 2.706 | 3.271 |
| 1.2 | -1.449 | -0.844 | -0.195 | 0.732 | 1.340 | 2.087 | 2.626 | 3.149 |
| 1.0 | -1.588 | -0.852 | $-0.164$ | 0.758 | 1.340 | 2.043 | 2.542 | 3.022 |
| 0.8 | -1.733 | -0.856 | $-0.132$ | 0.780 | 1.336 | 1.993 | 2.453 | 2.891 |
| 0.6 | -1.880 | -0.857 | -0.099 | 0.800 | 1.328 | 1.939 | 2.359 | 2.755 |
| 0.4 | -2.029 | -0.855 | -0.066 | 0.816 | 1.317 | 1.880 | 2.261 | 2.615 |
| 0.2 | $-2.178$ | -0.850 | -0.033 | 0.830 | 1.301 | 1.818 | 2.159 | 2.472 |
| 0 | -2.326 | -0.842 | 0 | 0.842 | 1.282 | 1.751 | 2.054 | 2.326 |
| -0.2 | -2.472 | $-0.830$ | 0.033 | 0.850 | 1.258 | 1.680 | 1.945 | 2.178 |
| -0.4 | -2.615 | $-0.816$ | 0.066 | 0.855 | 1.231 | 1.606 | 1.834 | 2.029 |
| -0.6 | -2.755 | -0.800 | 0.099 | 0.857 | 1.200 | 1.528 | 1.720 | 1.880 |
| -0.8 | -2.891 | $-0.780$ | 0.132 | 0.856 | 1.166 | 1.448 | 1.606 | 1.733 |
| -1.0 | -3.022 | $-0.758$ | 0.164 | 0.852 | 1.128 | 1.366 | 1.492 | 1.588 |
| $-1.2$ | $-3.149$ | -0.732 | 0.195 | 0.844 | 1.086 | 1.282 | 1.379 | 1.449 |
| -1.4 | $-3.271$ | $-0.705$ | 0.225 | 0.832 | 1.041 | 1.198 | 1.270 | 1.318 |
| $-1.6$ | $-3.388$ | $-0.675$ | 0.254 | 0.817 | 0.994 | 1.116 | 1.166 | 1.197 |
| -1.8 | -3.499 | -0.643 | 0.282 | 0.799 | 0.945 | 1.035 | 1.069 | 1.087 |
| $-2.0$ | -3.605 | -0.609 | 0.307 | 0.777 | 0.895 | 0.959 | 0.980 | 0.990 |
| -2.2 | $-3.705$ | $-0.574$ | 0.330 | 0.752 | 0.844 | 0.888 | 0.900 | 0.905 |
| -2.4 | -3.800 | -0.537 | 0.351 | 0.725 | 0.795 | 0.823 | 0.830 | 0.832 |
| -2.6 | -3.889 | -0.499 | 0.368 | 0.696 | 0.747 | 0.764 | 0.768 | 0.769 |
| $-2.8$ | -3.973 | -0.460 | 0.384 | 0.666 | 0.702 | 0.712 | 0.714 | 0.714 |
| -3.0 | -4.051 | -0.420 | 0.396 | 0.636 | 0.660 | 0.666 | 0.666 | 0.667 |

## K - Extreme Value Type I Distribution

| Table 11.8 | Probability |  |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | 0.2 | 0.1 | 0.067 | 0.05 | 0.04 | 0.02 | 0.0133 | 0.01 | 0.001 |
| Sample | Return Period |  |  |  |  |  |  |  |  |
| Size, $n$ | 5 | 10 | 15 | 20 | 25 | 50 | 75 | 100 | 1000 |
| 15 | 0.967 | 1.703 | 2.117 | 2.410 | 2.632 | 3.321 | 3.721 | 4.005 | 6.265 |
| 20 | 0.919 | 1.625 | 2.023 | 2.302 | 2.517 | 3.179 | 3.563 | 3.836 | 6.006 |
| 25 | 0.888 | 1.575 | 1.963 | 2.235 | 2.444 | 3.088 | 3.463 | 3.729 | 5.842 |
| 30 | 0.866 | 1.541 | 1.922 | 2.188 | 2.393 | 3.026 | 3.393 | 3.653 | 5.727 |
| 35 | 0.851 | 1.516 | 1.891 | 2.152 | 2.354 | 2.979 | 3.341 | 3.598 |  |
| 40 | 0.838 | 1.495 | 1.866 | 2.126 | 2.326 | 2.943 | 3.301 | 3.554 | 5.576 |
| 45 | 0.829 | 1.478 | 1.847 | 2.104 | 2.303 | 2.913 | 3.268 | 3.520 |  |
| 50 | 0.820 | 1.466 | 1.831 | 2.086 | 2.283 | 2.889 | 3.241 | 3.491 | 5.478 |
| 55 | 0.813 | 1.455 | 1.818 | 2.071 | 2.267 | 2.869 | 3.219 | 3.467 |  |
| 60 | 0.807 | 1.446 | 1.806 | 2.059 | 2.253 | 2.852 | 3.200 | 3.446 |  |
| 65 | 0.801 | 1.437 | 1.796 | 2.048 | 2.241 | 2.837 | 3.183 | 3.429 |  |
| 70 | 0.797 | 1.430 | 1.788 | 2.038 | 2.230 | 2.824 | 3.169 | 3.413 | 5.359 |
| 75 | 0.792 | 1.423 | 1.780 | 2.029 | 2.220 | 2.812 | 3.155 | 3.400 |  |
| 80 | 0.788 | 1.417 | 1.773 | 2.020 | 2.212 | 2.802 | 3.145 | 3.387 |  |
| 85 | 0.785 | 1.413 | 1.767 | 2.013 | 2.205 | 2.793 | 3.135 | 3.376 |  |
| 90 | 0.782 | 1.409 | 1.762 | 2.007 | 2.198 | 2.785 | 3.125 | 3.367 |  |
| 95 | 0.780 | 1.405 | 1.757 | 2.002 | 2.193 | 2.777 | 3.116 | 3.357 |  |
| 100 | 0.779 | 1.401 | 1.752 | 1.998 | 2.187 | 2.770 | 3.109 | 3.349 | 5.261 |
| $\infty^{\text {a }}$ | 0.719 | 1.305 | 1.635 | 1.866 | 2.044 | 2.592 | 2.911 | 3.137 | 4.936 |
| ${ }^{\text {a }}$ Additional data for $n=\infty$ : |  |  |  |  |  |  |  |  |  |
| Probability | K |  |  |  |  |  |  |  |  |
| 0.3 | 0.354 |  |  |  |  |  |  |  |  |
| 0.4 | 0.0737 |  |  |  |  |  |  |  |  |
| 0.5 | -0.164 |  |  |  |  |  |  |  |  |
| 0.6 | -0.383 |  |  |  |  |  |  |  |  |
| 0.8 | -0.821 |  |  |  |  |  |  |  |  |
| 0.9 | -1.100 |  |  |  |  |  |  |  |  |

## Generalized Skew Coefficient

- $G=W g_{s}+(1-W) g_{m}$
- $\mathrm{W}=\mathrm{V}\left(\mathrm{g}_{\mathrm{m}}\right) /\left[\mathrm{V}\left(\mathrm{g}_{\mathrm{s}}\right)=\mathrm{V}(\mathrm{gm})\right]$
- Where
- g = generalized skew coefficient
- W weighted factor
- $g_{s}$ sample skew coefficient
- $g_{m}$ map (regional) skew coefficient
- $\mathrm{V}(\quad)=$ mean squared error of the variable in parentheses


## Map Skew Coefficients: Log Annual Maximum Streamflow

Figure 11.7 Map skew coefficients of logarithmic annual maximum streamflow (Interagency Advisory Committee on Water Data, 1982).


## Confidence Limits: Error Limits

Table 11.10 Error Limits for Frequency Curve

| Years of <br> Record, $N$ | 0.1 | 1 | 10 | 50 | 90 | 99 | 99.9 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | 4.41 | 3.41 | 2.12 | 0.95 | 0.76 | 1.00 | 1.22 |
|  | 2.11 | 1.65 | 1.07 | 0.58 | 0.57 | 0.76 | 0.94 |
|  | 1.52 | 1.19 | 0.79 | 0.46 | 0.48 | 0.65 | 0.80 |
|  | 1.23 | 0.97 | 0.64 | 0.39 | 0.42 | 0.58 | 0.71 |
|  | 0.93 | 0.74 | 0.50 | 0.31 | 0.35 | 0.49 | 0.60 |
|  | 0.77 | 0.61 | 0.42 | 0.27 | 0.31 | 0.43 | 0.53 |
|  | 0.67 | 0.54 | 0.36 | 0.24 | 0.28 | 0.39 | 0.49 |
| 70 | 0.55 | 0.44 | 0.30 | 0.20 | 0.24 | 0.34 | 0.42 |
| 100 | 0.45 | 0.36 | 0.25 | 0.17 | 0.21 | 0.29 | 0.37 |
|  | 99.9 | 99 | 90 | 50 | 10 | 1 | 0.1 |

Percent Exceedance Frequency (at 95\% Level of Significance) ${ }^{\text {a }}$
${ }^{\text {a }}$ Chance of true value being greater than the value represented by the error curve.
Source: Beard (1962).

## Confidence Limits: Probability Adjustment

## Table 11.11 Error Limits and Probability Adjustments

| (a) $P_{\alpha}$ (\%) (select) | 0.1 | 1 | 10 | 50 | 90 | 99 | 99.9 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| (b) $5 \%$ level (from Table 11.10) | 1.11 | 0.88 | 0.58 | 0.36 | 0.39 | 0.54 | 0.67 |
| ( $N=24$ ) |  |  |  |  |  |  |  |
| (c) Error limit, $[(\mathrm{b}) \times \mathrm{S}]$ | 0.342 | 0.271 | 0.179 | 0.111 | 0.120 | 0.166 | 0.206 |
| (d) Log value $\left[X^{a}+(\mathrm{c})\right]$ |  | 4.702 | 4.452 | 4.077 | 3.627 | 3.175 |  |
| (e) Curve value, [log ${ }^{-1}$ (d)] (cfs) |  | 50,350 | 28,310 | 11,940 | 4240 | 1496 |  |
| (f) $95 \%$ level (from Table 11.10) | 0.67 | 0.54 | 0.39 | 0.36 | 0.58 | 0.88 | 1.11 |
| (g) Error limit, $[(\mathrm{f}) \times \mathrm{S}]$ | 0.206 | 0.166 | 0.120 | 0.111 | 0.179 | 0.271 | 0.342 |
| (h) Log value, $\left[X^{a}-(\mathrm{g})\right]$ |  | 4.265 | 4.153 | 3.855 | 3.328 | 2.738 |  |
| (i) Curve value, $\left[\mathrm{log}^{-1}(\mathrm{~h})\right]$ (cfs) |  | 18,410 | 14,220 | 7160 | 2130 | 550 |  |
| (j) $P_{N}$ (for $\left.N-1=23\right)$ | 0.29 | 1.58 | 11.0 | 50.0 | 89.0 | 98.42 | 99.71 |

(from Table 11.12)
$S=$ Standard deviation of flood sample
${ }^{\mathrm{a}}=$ Column 3 of Table 11.9

## Confidence Limits: P-adjustment for Small Samples

Table 11.12 $P_{\boldsymbol{n}}$ Versus $P_{\infty}$ for Normal Distribution (Percent) ${ }^{\text {a }}$ for Expected Probability Adjustment

|  | $P_{\infty}$ |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $N-1$ | 50 | 30 | 10 | 5 | 1 | 0.1 | 0.01 |
|  |  |  | Adjusted Probability, $P_{n}$ |  |  |  |  |
| 5 | 50.0 | 32.5 | 14.6 | 9.4 | 4.2 | 1.79 | 0.92 |
| 10 | 50.0 | 31.5 | 12.5 | 7.3 | 2.5 | 0.72 | 0.25 |
| 15 | 50.0 | 31.1 | 11.7 | 6.6 | 1.96 | 0.45 | 0.13 |
| 20 | 50.0 | 30.8 | 11.3 | 6.2 | 1.7 | 0.34 | 0.084 |
| 25 | 50.0 | 30.7 | 11.0 | 5.9 | 1.55 | 0.28 | 0.06 |
| 30 | 50.0 | 30.6 | 10.8 | 5.8 | 1.45 | 0.24 | 0.046 |
| 40 | 50.0 | 30.4 | 10.6 | 5.6 | 1.33 | 0.20 | 0.034 |
| 60 | 50.0 | 30.3 | 10.4 | 5.4 | 1.22 | 0.16 | 0.025 |
| 120 | 50.0 | 30.2 | 10.2 | 5.2 | 1.11 | 0.13 | 0.017 |
| $\propto$ | 50.0 | 30.0 | 10.0 | 5.0 | 1.0 | 0.10 | 0.01 |

[^0]
## Log-Pearson Type III Curve: Example 11.6 with Confidence limits

Figure 11.8 Log-Pearson type III frequency curve and a reliability band.


## Estimation of PMP <br> US National Weather Service

Figure 11.10 All-season PMP (in.) for $200 \mathrm{mi}^{2}, 24 \mathrm{hr}$.


## Depth-Area-Duration Relation Probable Maximum Precipitation (PMP)

| Table 11.14 Storm Area |  | Depth-Area-Duration Relation of Maximum Probable Precipitation ${ }^{\text {a }}$ |  |  |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  | $-\begin{gathered} \text { Duration } \\ (\mathrm{hr}) \end{gathered}$ | Regions |  |  |  |  |  |  |  |  |
| $\mathrm{mi}^{2}$ | km ${ }^{2}$ |  | 1 | 11 | III | IV | Va | Vb | VI | VIla | VIlb |
| 10 | 26 | 6 | 1.00 | 1.09 | 1.03 | 0.93 | 1.04 | 1.01 | 0.90 | 1.04 | 1.00 |
|  |  | 12 | 1.20 | 1.29 | 1.22 | 1.10 | 1.26 | 1.18 | 1.07 | 1.21 | 1.16 |
|  |  | 24 | 1.28 | 1.38 | 1.31 | 1.25 | 1.34 | 1.31 | 1.25 | 1.34 | 1.33 |
|  |  | 48 | 1.38 | 1.50 | 1.45 | 1.40 | 1.50 | 1.45 | 1.40 | 1.50 | 1.45 |
|  |  | 72 | 1.47 | 1.60 | 1.55 | 1.50 | 1.52 | 1.53 | 1.50 | 1.52 | 1.53 |
| 200 | 518 | 6 | 0.75 | 0.78 | 0.74 | 0.66 | 0.76 | 0.72 | 0.67 | 0.73 | 0.68 |
|  |  | 12 | 0.90 | 0.93 | 0.87 | 0.82 | 0.93 | 0.86 | 0.81 | 0.87 | 0.85 |
|  |  | 24 | 1.00 | 1.00 | 1.00 | 1.00 | 1.00 | 1.00 | 1.00 | 1.00 | 1.00 |
|  |  | 48 | 1.10 | 1.12 | 1.14 | 1.16 | 1.13 | 1.14 | 1.16 | 1.17 | 1.15 |
|  |  | 72 | 1.15 | 1.20 | 1.20 | 1.22 | 1.22 | 1.23 | 1.23 | 1.23 | 1.25 |
| 1,000 | 2,590 | 6 | 0.57 | 0.56 | 0.54 | 0.50 | 0.56 | 0.52 | 0.50 | 0.52 | 0.52 |
|  |  | 12 | 0.67 | 0.71 | 0.66 | 0.63 | 0.70 | 0.69 | 0.63 | 0.63 | 0.66 |
|  |  | 24 | 0.77 | 0.80 | 0.79 | 0.79 | 0.80 | 0.79 | 0.83 | 0.80 | 0.80 |
|  |  | 48 | 0.85 | 0.90 | 0.92 | 0.93 | 0.90 | 0.92 | 0.94 | 0.93 | 0.93 |
|  |  | 72 | 0.96 | 0.97 | 0.98 | 1.00 | 0.97 | 0.98 | 1.04 | 0.98 | 0.98 |
| 5,000 | 12,950 | 6 | 0.36 | 0.36 | 0.31 | 0.28 | 0.36 | 0.31 | 0.28 | 0.33 | 0.31 |
|  |  | 12 | 0.45 | 0.47 | 0.43 | 0.39 | 0.48 | 0.43 | 0.40 | 0.45 | 0.43 |
|  |  | 24 | 0.52 | 0.54 | 0.54 | 0.55 | 0.54 | 0.54 | 0.55 | 0.56 | 0.56 |
|  |  | 48 | 0.63 | 0.67 | 0.68 | 0.65 | 0.67 | 0.65 | 0.68 | 0.70 | 0.69 |
|  |  | 72 | 0.70 | 0.74 | 0.76 | 0.76 | 0.74 | 0.76 | 0.78 | 0.74 | 0.76 |
| 10,000 | 25,900 | 6 | 0.26 | 0.27 | 0.23 | 0.21 | 0.28 | 0.23 | 0.22 | 0.28 | 0.23 |
|  |  | 12 | 0.36 | 0.37 | 0.33 | 0.30 | 0.38 | 0.35 | 0.32 | 0.37 | 0.35 |
|  |  | 24 | 0.42 | 0.45 | 0.43 | 0.43 | 0.47 | 0.44 | 0.45 | 0.47 | 0.45 |
|  |  | 48 | 0.50 | 0.58 | 0.54 | 0.55 | 0.58 | 0.57 | 0.58 | 0.60 | 0.60 |
|  |  | 72 | 0.60 | 0.62 | 0.64 | 0.65 | 0.66 | 0.64 | 0.67 | 0.67 | 0.65 |
| $20,000$ | 51,800 | 6 | 0.18 | 0.20 | 0.17 | 0.16 | 0.20 | 0.17 | 0.16 | 0.20 | 0.16 |
|  |  | 12 | 0.27 | 0.28 | 0.25 | 0.23 | 0.30 | 0.28 | 0.25 | 0.33 | 0.28 |
|  |  | 24 | 0.35 | 0.36 | 0.35 | 0.32 | 0.38 | 0.36 | 0.36 | 0.40 | 0.37 |
|  |  | 48 | 0.45 | 0.47 | 0.45 | 0.45 | 0.48 | 0.47 | 0.48 | 0.50 | 0.49 |
|  |  | 72 | 0.50 | 0.55 | 0.55 | 0.55 | 0.56 | 0.55 | 0.56 | 0.57 | 0.55 |
| ${ }^{\text {a }}$ Factors derived by the author from the figures in National Weather Service (1978) to be applied to 24 -hour values on $200-\mathrm{mi}^{2}$ area of Figure 11.10. |  |  |  |  |  |  |  |  |  |  |  |


[^0]:    ${ }^{\text {a }}$ Values for probability $>50$ by subtraction from 100 [i.e., $P_{90}=\left(100-P_{10}\right)$ ].
    Source: Beard (1962).

